

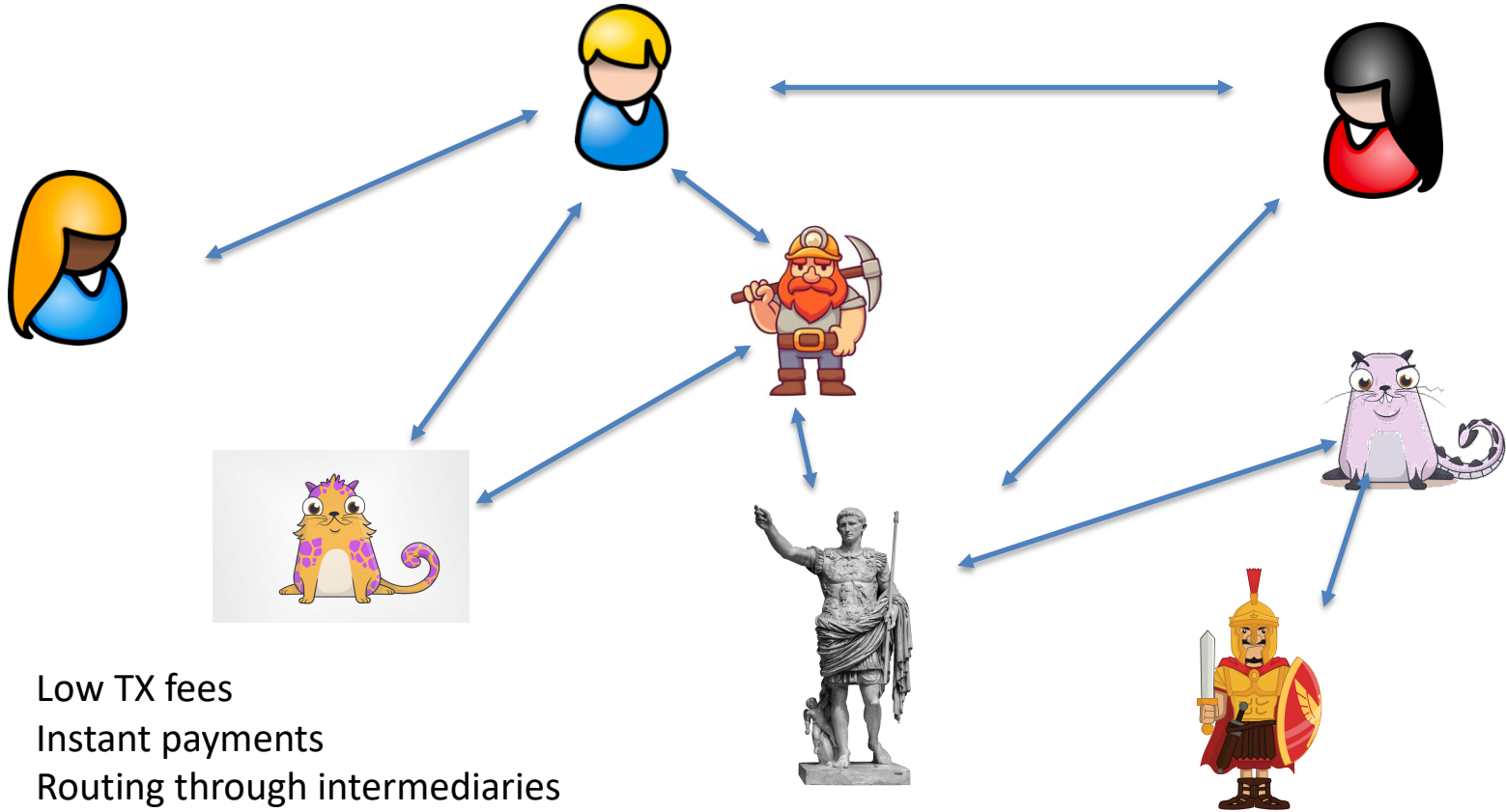
CS251 Fall 2021  
([cs251.stanford.edu](https://cs251.stanford.edu))



# Scaling II: Rollup

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# Lightning network



- Low TX fees
- Instant payments
- Routing through intermediaries

# Downsides of Payment/State Channels

- Everyone needs to be online
  - Mitigated by watchtowers
  - Hubs need to be online
- Capital is locked up
  - Funds in one channel can't be used in different channel
  - If network is separated transactions are not possible
- Only Peer to Peer payments
  - No multi party contracts channels
- TX to fund/close

# Blockchain Layers

Layer 3:

**user facing tools** (cloud servers)

Layer 2:

**applications** (DAPPs, smart contracts)

Layer 1.5:

**compute layer** (blockchain computer)

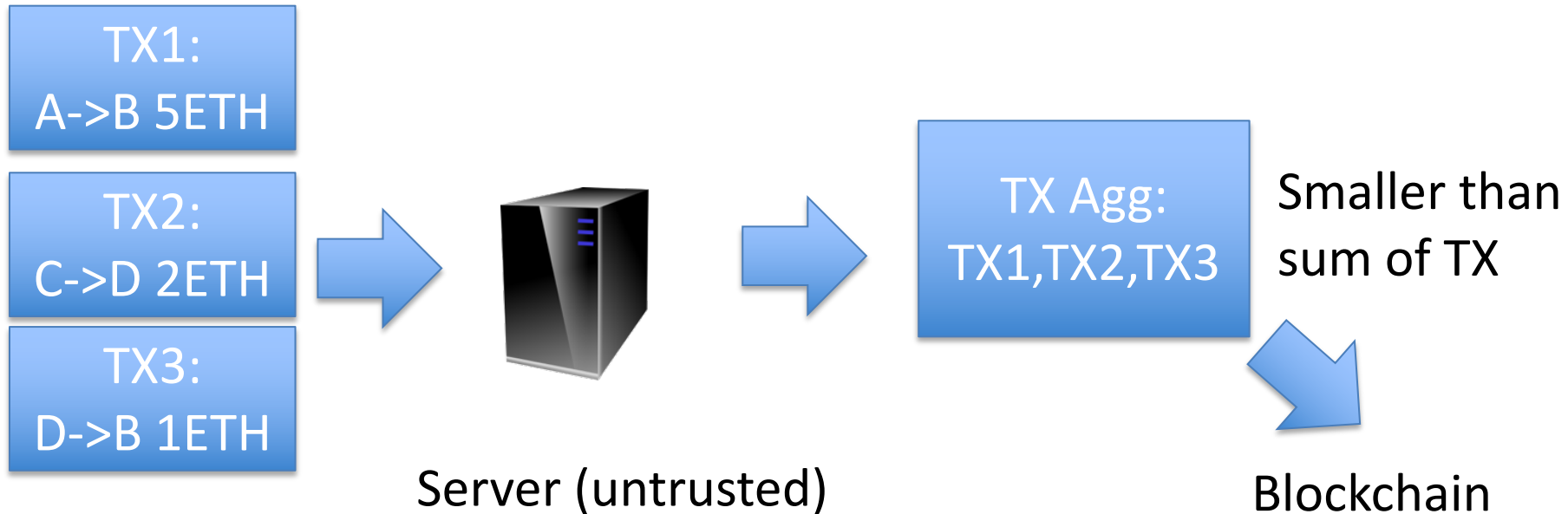
Layer 1:

**consensus layer**

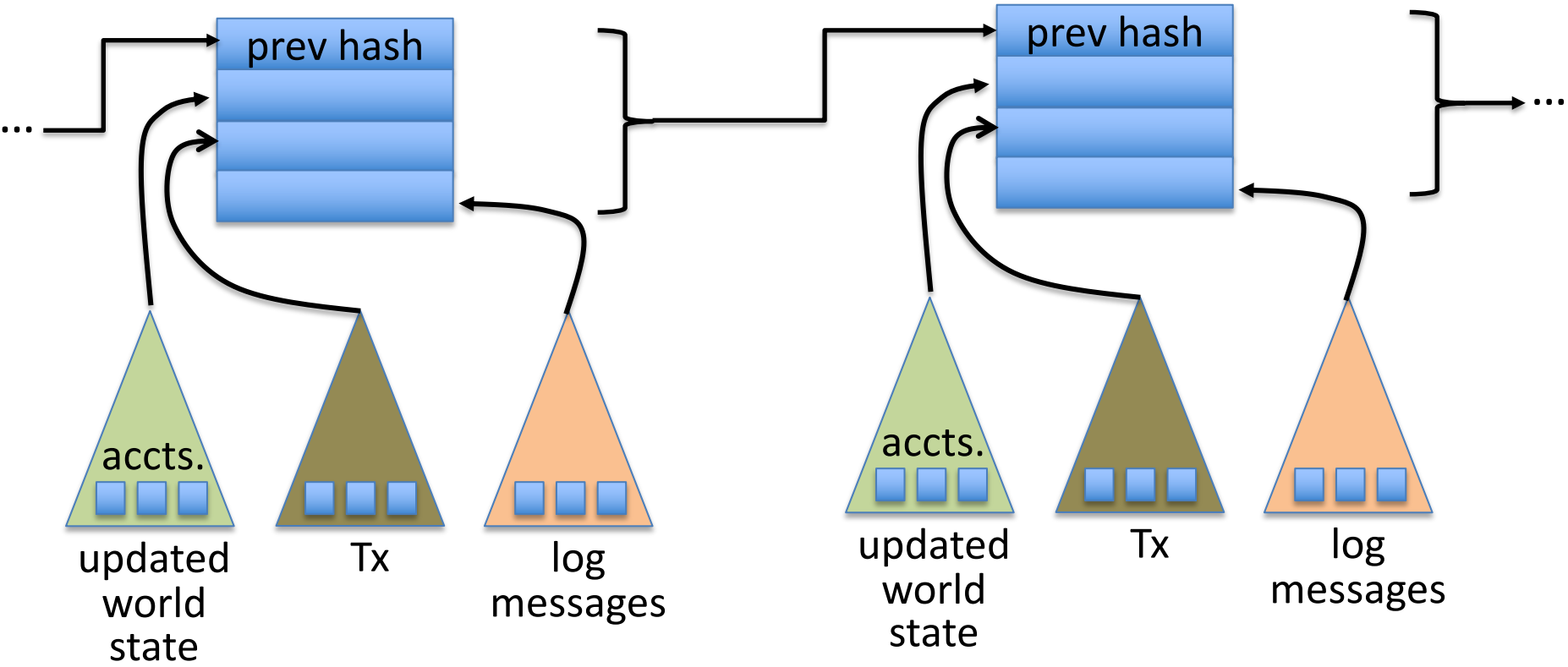
Bitcoin/Ethereum combine ordering (layer 1) and verification (1.5)  
What if we can outsource verification? Makes consensus cheaper

# Idea: Aggregate Transactions

- Payment channels move more transactions offchain
- Idea: Combine Transaction, Rollup Server verifies



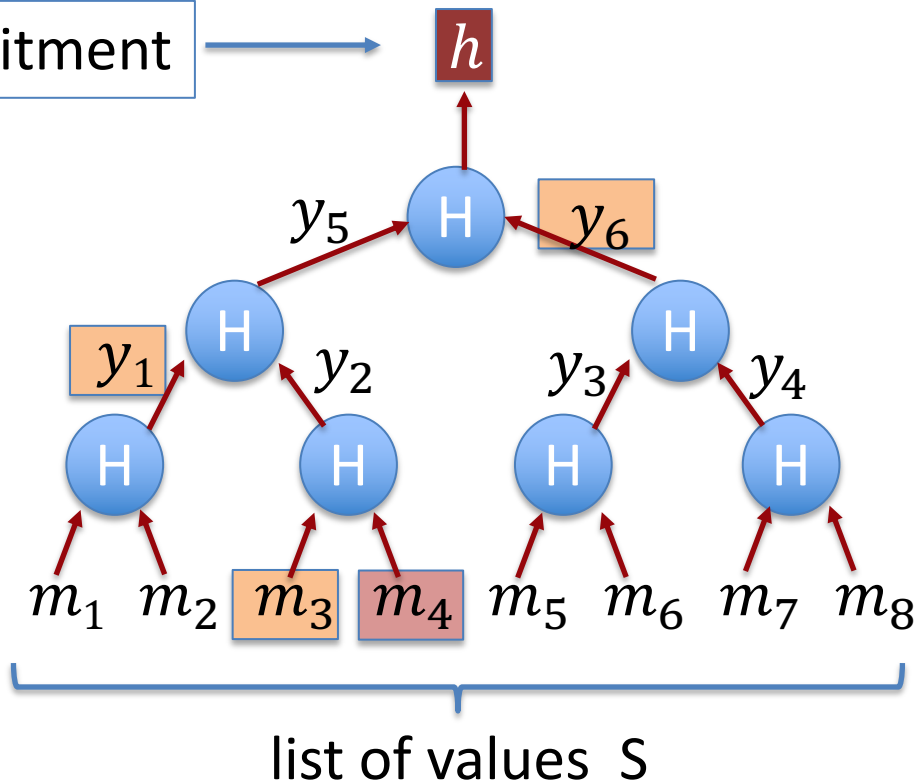
# Recap: The Ethereum blockchain



# Recap: Merkle tree

(Merkle 1989)

commitment



Goal:

- commit to list  $S$
- Later prove  $S[i] = m_i$

To prove  $S[4] = m_4$  ,  
proof  $\pi = (m_3, y_1, y_6)$

length of  $\pi$ :  $\log_2 |S|$

# Recap State Commitment

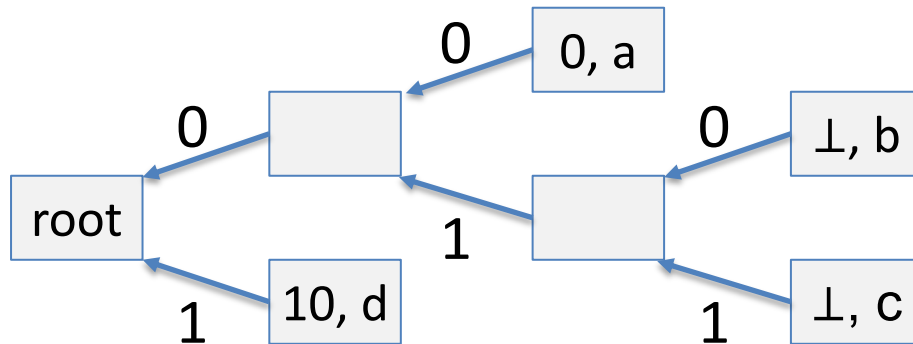
Every contract has an associated **storage array S[]**:

**S[0], S[1], ... , S[2<sup>256</sup>-1]**: each cell holds 32 bytes, init to 0.

Account storage root: **Merkle Patricia Tree hash** of S[]

- Cannot compute full Merkle tree hash: 2<sup>256</sup> leaves

S[000] = a  
S[010] = b  
S[011] = c  
S[110] = d



time to compute  
root hash:  
 $\leq 2 \times |S|$

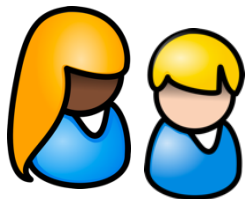
$|S|$  = # non-zero cells



# Merke (Patricia) Tree Proofs

- Logarithmic in tree height
- Given proof for  $i$   $\rightarrow$  Possible to update  $S[i]$  and recompute root
- Given proof for  $i$ , proof for  $j$  and update of  $S[j]$  it's possible to update proof for  $S[i]$
- Exclusion proofs possible in Patricia Trees

# Rollup



Users



Server

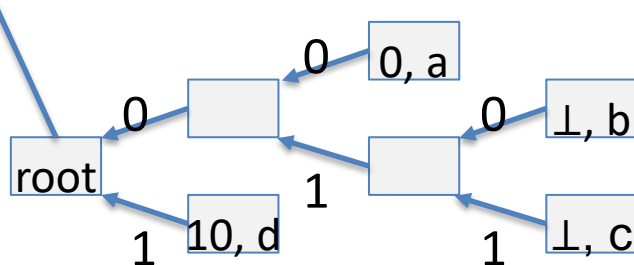


Rollup Smart Contract

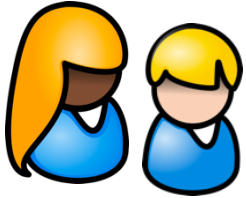
## Rollup State S

$S[A's\ PK] = \{3\ \text{ETH},\ \text{nonce}\}$   
 $S[B's\ PK] = \{2\ \text{ETH},\ \text{nonce}\}$   
 $S[C's\ PK] = \{10\ \text{ETH},\ \text{nonce}\}$   
 $S[D's\ PK] = \{1\ \text{ETH},\ \text{nonce}\}$

## Stores S



# Rollup Deposit



TX Deposit



Rollup Smart Contract `root`

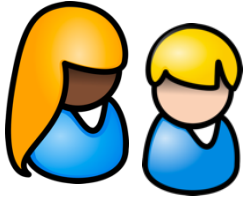
Users

TX Deposit:

Proof that  $A$ 's PK  $\notin S$  given `root`  
3 ETH transfer

1. Checks Proof
2. Updates root such that  $S[A\text{'s PK}] = \{3 \text{ ETH}, 0\}$

# Rollup Withdraw



TX Withdraw



Rollup Smart Contract `root`

Users

TX Withdraw:

Proof that  $S[A's\ PK]=\{3\ ETH, nonce\}$

given `root`

Destination Address NewA

Signature by A

1. Checks Proof
2. Checks Signature
3. Sends 3 ETH to NewA

# Rollup Transfer



TX Transfer



Space saved but  
no computation

Users

TX Transfer:

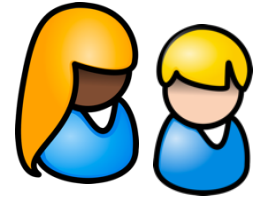
Proof that given `root`  
 $S[A's\ PK]=\{3\ ETH, 0\}$   
 $S[B's\ PK]=\{2\ ETH, 0\}$   
Transfer amount 2 ETH  
Signature by A

Rollup Smart Contract `root`

1. Checks Proofs
2. Checks Signature
3. Set
  1.  $S[A's\ PK]=\{1\ ETH, 1\}$
  2.  $S[B's\ PK]=\{4\ ETH, 1\}$

# SNARK

```
3 function validatePatriciaProof(  
4   bytes32 rootHash,  
5   bytes memory key,  
6   bytes memory value,  
7   bytes[] memory path  
8 ) pure returns (bool accept) {  
9   uint256 k = keccak256(key);  
10  }
```



Provides Proof/SNARK that given given public inputs (rootHash, key, value) it knows private inputs (path) such that function outputs true

**SNARK is short/easy to check**

# SNARK: a Succinct ARgument of Knowledge

A succinct preprocessing argument system is a triple  $(S, P, V)$ :

- $S(C) \rightarrow$  public parameters  $(S_p, S_v)$

$|\pi| = 500$  bytes  
 $\text{time}(V) = 500k$  Gas

```
3 function validatePatriciaProof(proof  $\pi$  ;  
4     bytes32 rootHash,  
5     bytes memory key,  
6     bytes memory value,  
7     bytes[] memory path) bool verify ;  
8 ) pure returns (bool accept) {  
9     uint256 k = 0; if (key[k] == 0) {
```

$|\pi| = O(\log(|C|), \lambda)$

$\text{time}(V) = O(|x|, \log(|C|), \lambda)$

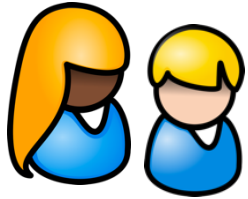
If  $(S, P, V)$  is **succinct** and **zero-knowledge** then we say that it is a **zk-SNARK**

# ZKRollup

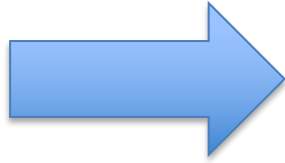
- Merkelize Transactions
- SNARK proves that given transactions I know signatures such that state transition  $S \rightarrow S'$  valid
- Publish transaction diff on chain.
- No signatures per transaction.
- 500k gas + data cost for on chain diff



# ZKRollup (Validity Rollup)



Users



Transactions



Server  
Stores  $S$



$root'$

$\pi$



Rollup Smart Contract

$root$

Commitment to  $S$

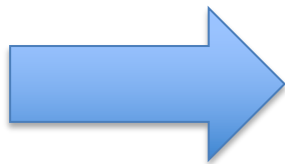
Coordinator does:

1. Applies TXs to  $S$  resulting in  $S'$
2. Produces  $root' = \text{Commit}(S')$
3. Produces SNARK  $\pi$  that  $\exists txs$  such that  $root'$  is correct update to state  $S$  committed in  $root$

# ZKRollup



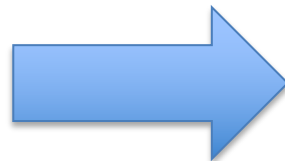
Users



Transactions



Server  
Stores  $S'$



$root'$

$\pi$



Rollup Smart Contract

$root'$

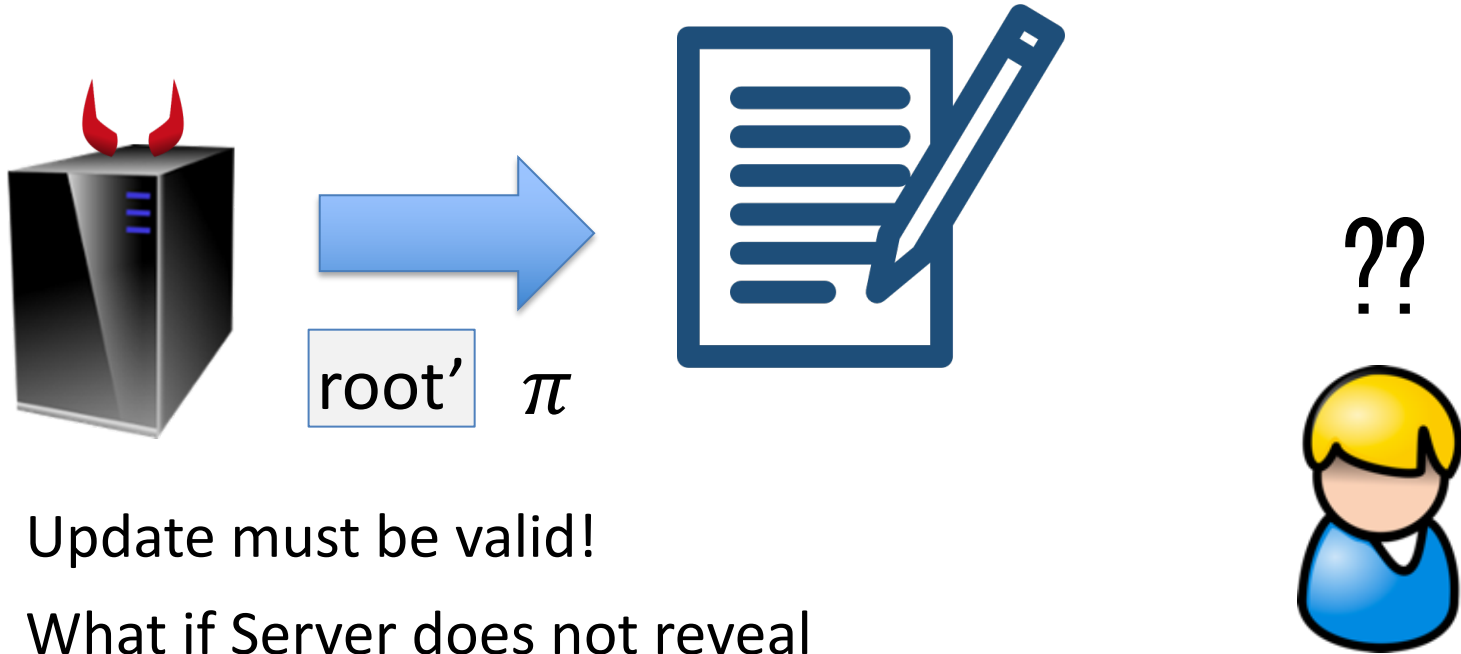
Commitment to  $S$

Smart Contract does:

1. Verify  $\pi$  given  $root$  and  $root'$
2. If accept then set  $root \leftarrow root'$

Smart contract still allows “manual” withdrawals

# Data Availability Problem

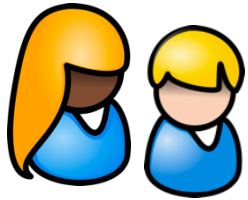


Update must be valid!

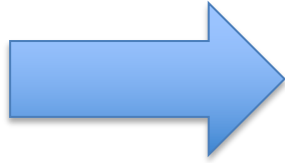
What if Server does not reveal  
data?

Can't update Merkle proofs  
Can't withdraw!

# Publish diff on chain



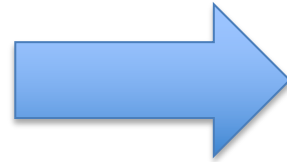
Users



Transactions  
with signatures



Server  
Stores  $S'$



$root'$

$\pi$  txlist



Rollup Smart Contract

$root'$

Txlist= [{A-> B 3}, {C-> D 2}, {D-> B 1}]

No signatures, Sender, Receiver, Amount only in Calldata (not stored)

<100bytes per tx ~400 gas/tx, SNARK verification ~1500 gas/tx (if full)

Full Block 3600 rollup tx vs 570 normal tx (6x speedup)

# zkRollup stats

- ZKRollup is cheaper than onchain tx
- Can scale to max  $\sim 300$ tx/s now,  $1000$ tx/s soon
- Vs. max  $40-50$ tx/s on mainnet
- Cost dominated by SNARK verification
  - Will get cheaper precompiles
- Finality  $\sim$  Blockchain finality (no instant transfer)

# Multiple Assets

Very easy to support many assets

Simply add asset field to TX

Hardly increases SNARK complexity

Txlist= [{A-> B 3 ETH}, {C-> D 2 DAI}, {D-> B 1 BAT}]

1 byte → 256 assets

2 bytes → 65k assets

# Transaction List/Atomic Swaps

Support transaction list that are executed together  
Transactions need to be signed by all senders  
Can't execute part of transaction only all together!

Enables atomic swaps: Alice swaps with Bob 3 ETH for 2 DAI  
Txlist= [{A-> B 3 ETH and B-> A 2 DAI}, {D-> B 1 BAT}]

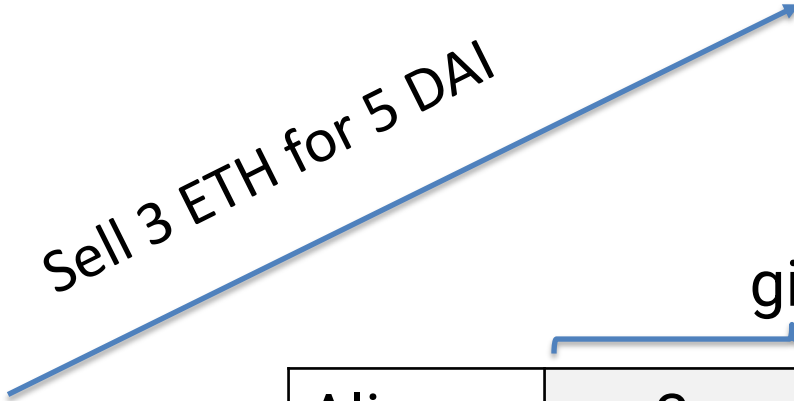
# Exchanges



Buy 3 ETH for 5 DAI



Sell 3 ETH for 5 DAI



Exchanges match orders

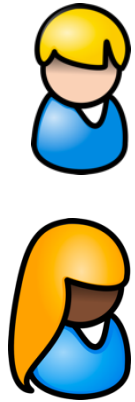
Classical exchanges also store funds

Order book

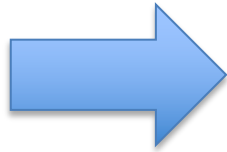
	give		get	
Alice	3	ETH	5	DAI
Bob	5	DAI	3	ETH
Carol	4	BAT	10	DAI



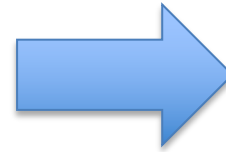
# Rolled up Exchange



Submit orders



Has orderbook  
Matches orders  
Rolls up  
transactions as  
atomic swaps



Txs Root,  $\pi$

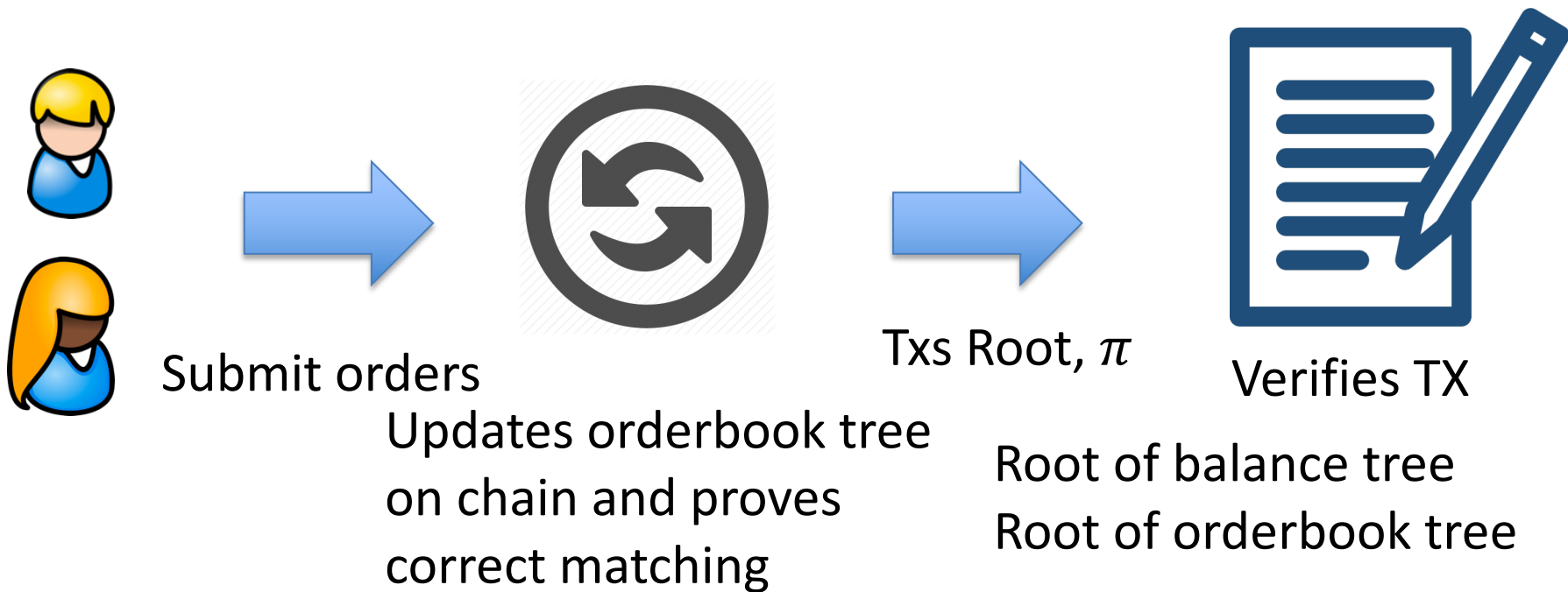


Verifies TX

Root of balance tree

Exchange trusted for  
honest matching

# Rolled up Exchange v2



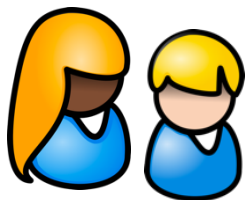
Benefit: No trust

Downside: Every order creates rollup TX, No instant matching

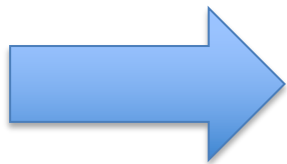
# Rolling up Smart Contracts

- zkRollup works best for simple transfers
- zkRollup for the EVM?
  - Roll up generic smart contract transactions?
  - Create SNARK where the circuit implements the EVM
  - More expensive on the server
  - Soon to be a reality for a subset of the EVM (zkEVM)
- Can we support smart contract rollups today?

# Optimistic Rollup



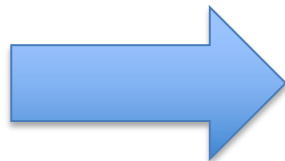
Users



Transactions  
with signatures



Server  
Stores  $S'$



$root'$

$\pi$  txlist



Rollup Smart Contract

$root'$

What if we remove the SNARK?

Idea: Instead of proving correctness, prove fraud!

New Role: Validator checks correctness, provides fraud proofs



# Optimistic Rollup

- Server updates transaction root
- Server puts a large bond into escrow
- If transaction update is invalid users/validators provide *fraud proof*
- Successful fraud proof means bond gets *slashed*
  - Part to validator providing proof part gets burned
- Unsuccessful fraud proof costs validator money
- **How to proof fraud?**

# Fraud Proofs



Server

root

Commits to state  $S$

txlist

root'



Validator

1. Stores  $S$  agrees on root
2. Applies txlist to  $S$  to compute  $S'$
3. Computes root'' from  $S'$
4. If  $\text{root}' \neq \text{root}''$  call "Fraud"

Problem: Validator doesn't know what's in root'

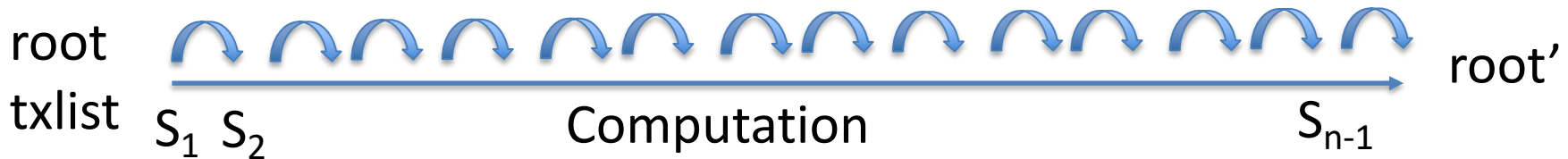
# Referee Delegation

Idea: Server and Validator find first point of disagreement



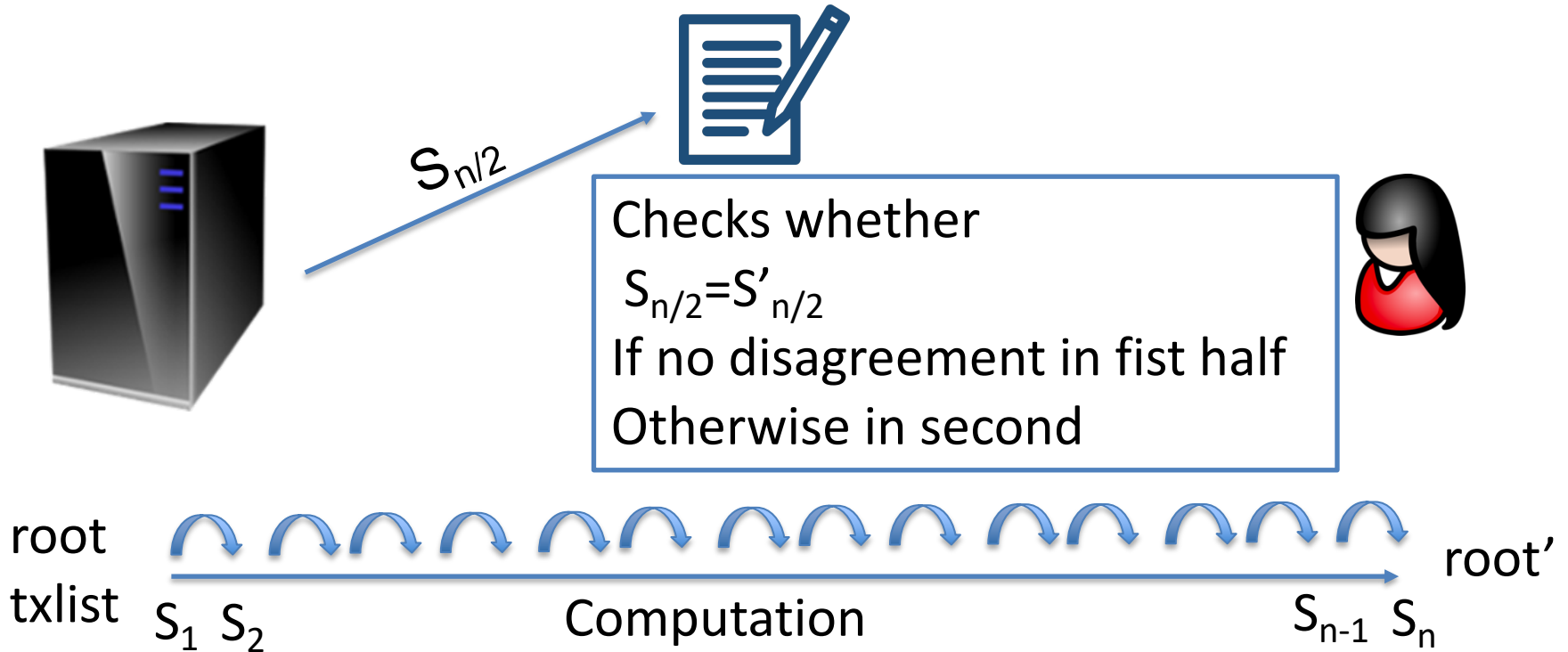
Break down computation of  $S'$  into small steps, e.g. cycles on a VM  
Validator does the same

Let  $S_i$  be Server's intermediate states and  $S'_i$  the validator's



# Referee Delegation

Server and Validator run interactive binary search





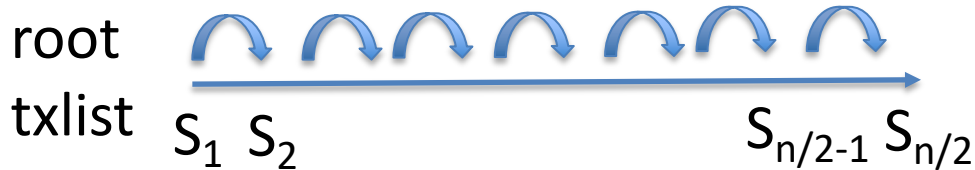
# Referee Delegation



Repeat protocol for  $\log_2(n)$  steps  
End with agreement on  $S_i$  and  
disagreement on  $S_{i+1}$  and  $S'_{i+1}$



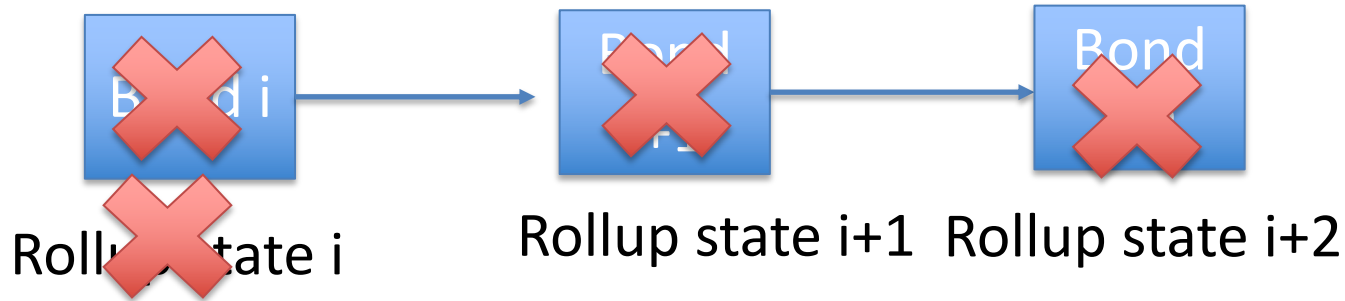
Smart Contract checks transition between  $S_i$   
and  $S_{i+1}$  and declares winner



# Problem: Checks take a long time

- $\log_2(n)$  messages (1 hash per message)
- 1 Verification step on smart contract
- If either party timeouts declares winner
- Loser gets *slashed*, Winner rewarded
- Problem:  $\log_2(n)$ \*timeout
- No incentive to cheat
- But: Long wait till finalization! (7 days)

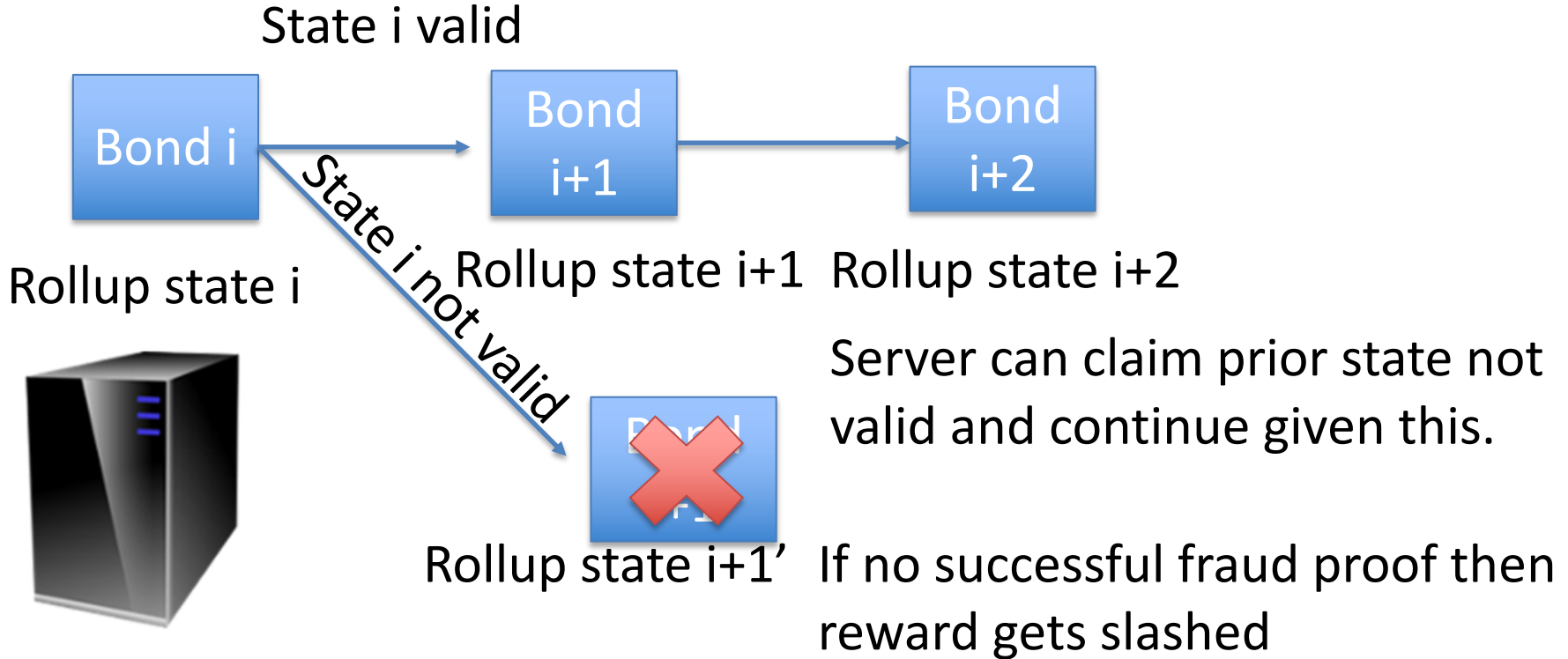
# Pipelined Assertions



Server can build on states  
before timeouts

If prior state invalid, all  
subsequent bonds are slashed

# Pipelined Assertions



# Insurance of Rollup -> Instant Finality

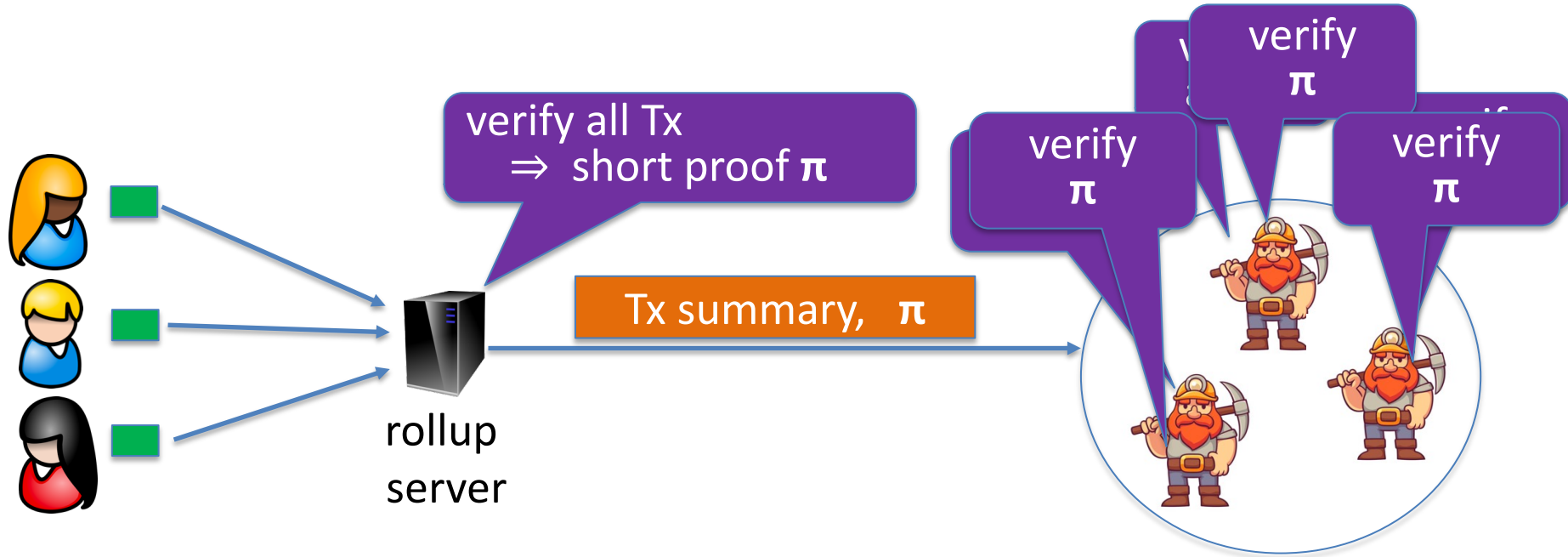
- Rollup is not instant (unlike lightning)
- But if server is trusted then giving them transaction -> finality
- Idea: Use insurance to achieve finality
- Server signs insurance
- If transaction not included in next (few) blocks insurance can be used to get insurance premium
- Works for zk and optimistic rollup
- Does not work for NFTs (directly)

# Optimistic Rollup

- Live and implemented (Optimism and Arbitrum)
- You can port arbitrary smart contracts (OVM)
- Works well if honest rollup server
  - Fraud proofs protection if malicious server
- Up to ~4000 tx/s on ETH 1.0
- Important that one independent validator exists
- 7 day finality wait

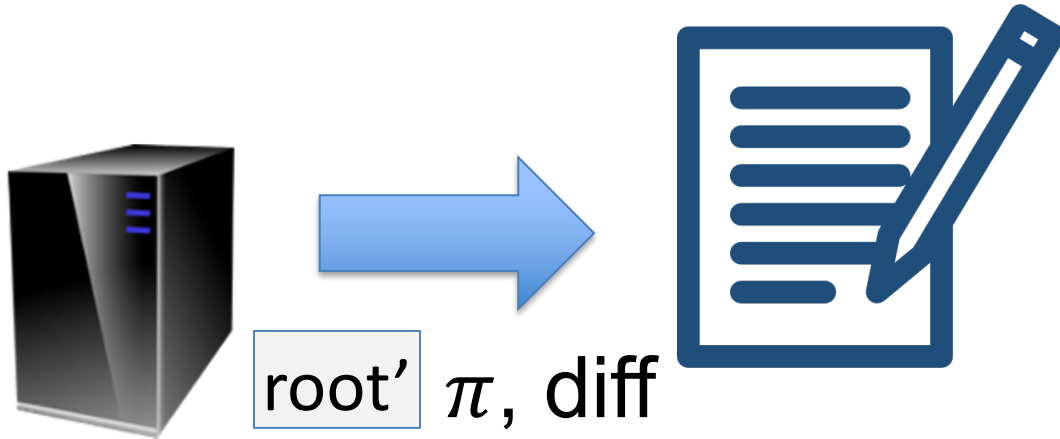
# A combined view of rollups

Standard L1 chains: every miner must verify every posted Tx



Rollup server: compresses a thousand Tx into one on-chain proof (SNARK or Fraud)

# Data Availability



Update must be valid!

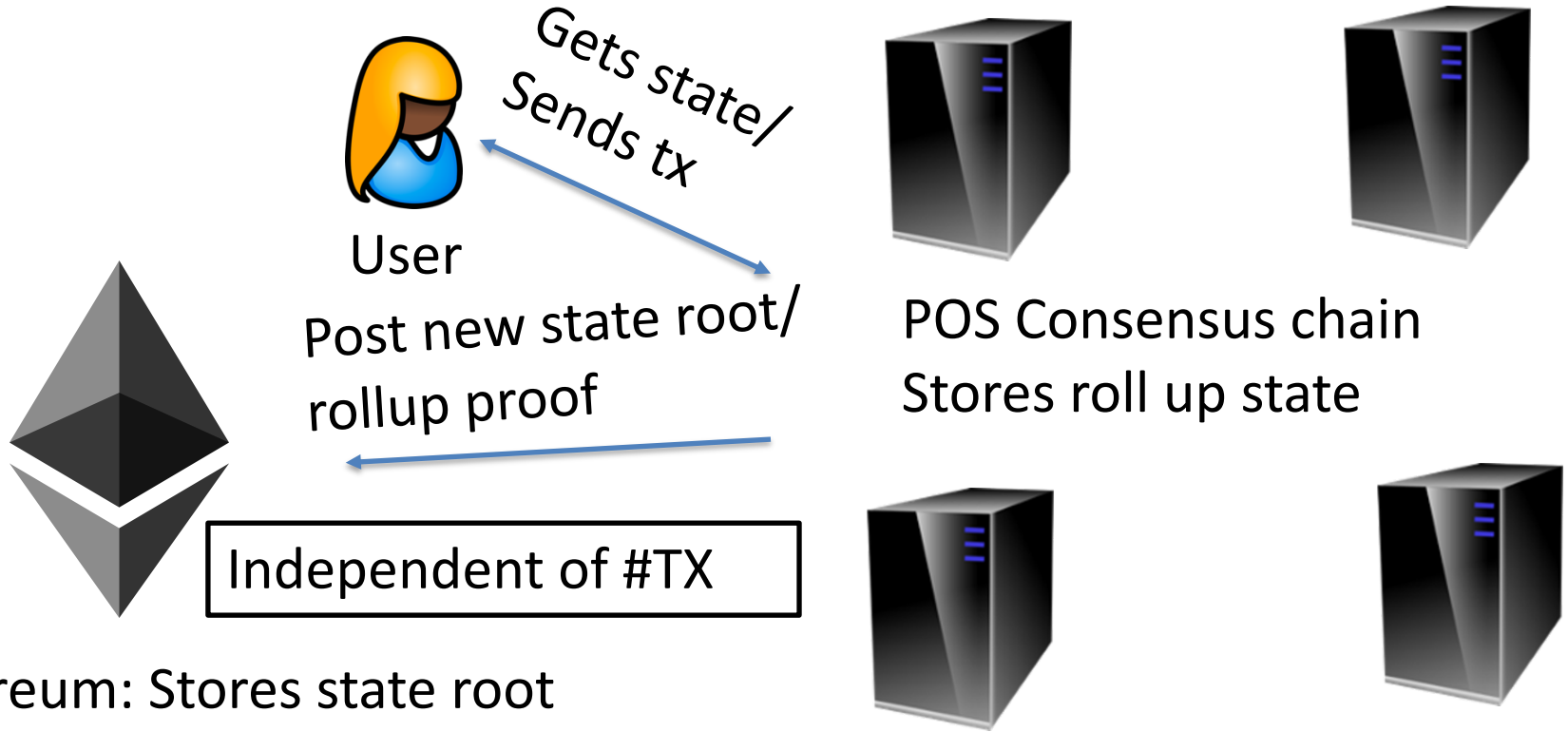
User must know state transition  
Posting state diff on chain limits  
rollup benefits

Can we keep the  
data off chain?



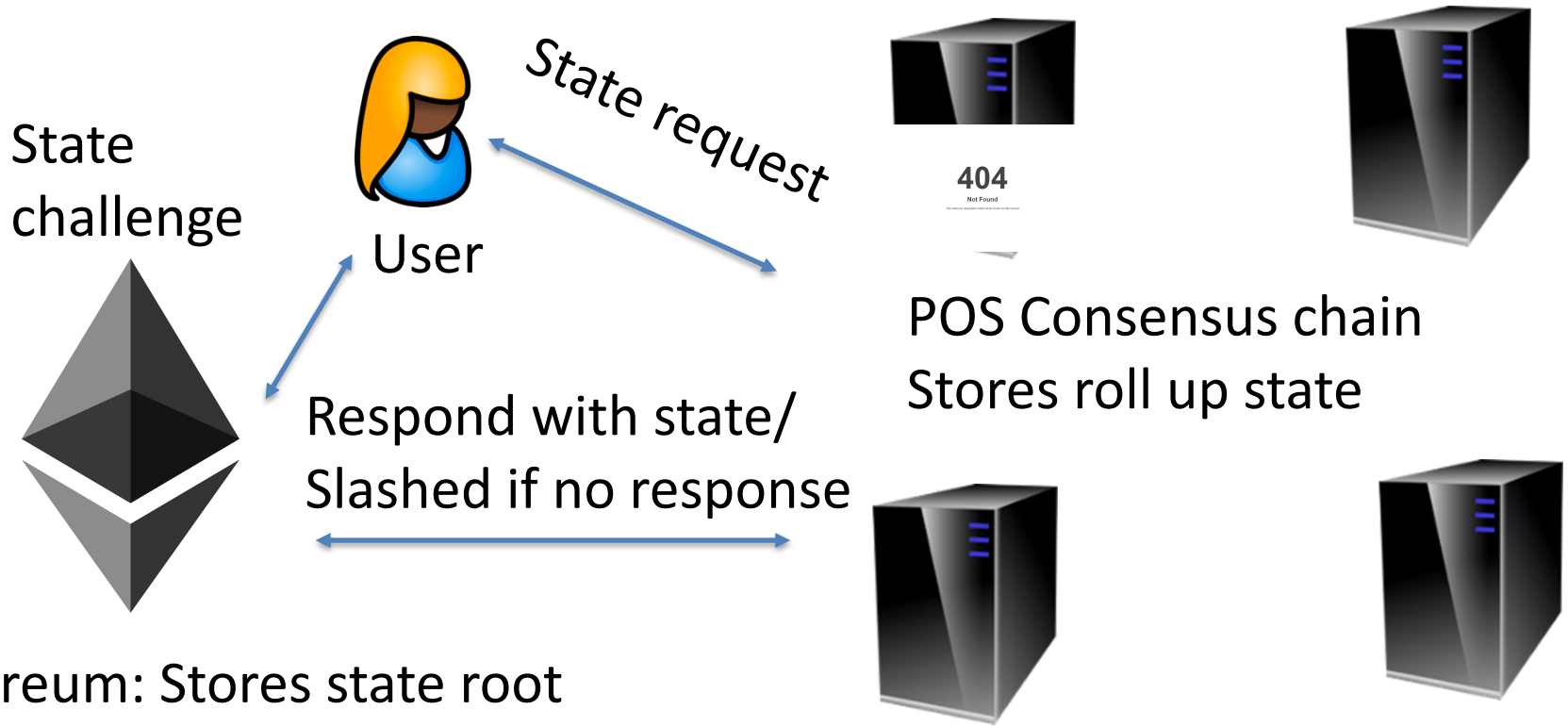
# Off Chain Rollups (Validum and Plasma)

- Idea: Create a separate “cheap” chain for the data



# Conflict Resolution: On Chain requests

- Idea: Create a separate “cheap” chain for the data



# On Chain vs Off Chain Data availability

- Off Chain is much **cheaper** and independent of #tx
  - Only limitation is data consensus
- Data consensus **not trusted** for security
  - Can't steal your money
- Data consensus **is trusted** for availability
  - Can lock up your money (bribery attack)
  - Can increase fees
- Economic incentives can mitigate issues
- For high value transfer use on chain rollup for low value use off chain rollup

# 2 by 2 rollup

Scaling the blockchain: Payment channels and Rollups (L2 scaling)

		SNARK validity proofs	Fraud proofs
security			
availability	Tx summary on L1 chain	zkRollup blockchain finality, only simple transfers (now)	optimistic Rollup 7 day finality Instant transfers
	Tx summary off chain	Vallidium large #tx but vulnerable to lock up attacks	"Plasma" Largest #tx but lock up attacks and long finality

END OF LECTURE

Next lecture: Recursive SNARKs