

Decentralized Exchange & Lending

Ali Yahya & Eddy Lazzarin

a16z

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Decentralized Exchanges (DEXs)

Ali Yahya

DEXs: Why do they matter?

- Enable Protocol Composability

<rant>

</rant>

- Non-Custodial
- Have Global Reach

11,354.04 USDLast trade price-0.33%24h price6,550 BTC24h volume

Order Book

Market Size	Price (USD)	My Size
0.6100	11368.39	-
3.6800	11367.07	-
0.3000	11366.94	-
0.2639	11366.34	-
1.1745	11365.00	-
3.3100	11364.60	-
0.2500	11363.78	-
0.9613	11363.00	-
0.8696	11362.30	-
0.2200	11362.29	-
1.2241	11361.83	-
3.5000	11361.43	-
0.4565	11361.42	-
0.8693	11360.75	-
11.9372	11360.70	-
0.3422	11360.39	-
0.2805	11360.38	-
0.2641	11359.53	-
0.1000	11359.21	-
3.5000	11359.11	-
0.8696	11359.06	-
3.6000	11358.35	-
0.7719	11358.31	-
0.0500	11357.29	-
0.3180	11357.18	-
3.5400	11356.96	-
0.8698	11356.95	-
0.2642	11356.68	-
0.2000	11356.60	-
4.2000	11356.53	-
2.0000	11356.28	-
0.4369	11355.55	-
0.0200	11355.54	-
0.1740	11354.62	-
0.2000	11354.38	-
1.3200	11354.33	-
0.1000	11354.22	-
7.6011	11354.04	-

USD Spread0.01

0.0014	11354.03	-
0.0984	11353.56	-
0.0500	11353.55	-
0.2000	11351.88	-
1.3200	11350.10	-
0.0337	11350.06	-
0.1748	11350.05	-
0.5000	11349.88	-
0.1000	11349.82	-
0.0200	11348.88	-
0.4804	11348.87	-
0.1997	11348.86	-
0.4369	11348.66	-
0.3000	11348.64	-
2.9290	11348.61	-
0.3230	11348.05	-
1.4666	11347.97	-

Aggregation0.01

Price Charts

5mCandleOverlay

O: 11,360.65H: 11,363.00L: 11,353.28C: 11,354.04V: 14

11,354.035Mid Market Price

Open Orders

Side	Size	Filled (BTC)	Price (USD)	Fee (USD)	Status
No orders to show					

GET STARTED

orLog in

Fills

Side	Size (BTC)	Price (USD)	Fee (USD)	Time
No fills to show				

Trade History

Trade Size	Price (USD)	Time
0.0012	11354.04 ↗	12:28:39
0.0216	11354.04 ↗	12:28:39
0.0086	11354.03 ↘	12:28:37
0.0127	11354.04 ↗	12:28:36
0.0950	11354.04 ↗	12:28:31
0.0063	11354.04 ↗	12:28:32
0.0017	11354.04 ↗	12:28:29
0.0173	11354.04 ↗	12:28:29
0.0820	11354.04 ↗	12:28:27
0.0028	11354.04 ↗	12:28:27
0.0190	11356.84 ↗	12:28:20
0.0031	11357.15 ↗	12:28:19
0.0021	11357.15 ↗	12:28:19
0.0451	11356.70 ↘	12:28:18
0.0259	11357.39 ↗	12:28:16
0.0718	11357.22 ↗	12:28:16
0.0042	11355.06 ↗	12:28:14
0.0173	11354.57 ↗	12:28:13
0.0031	11354.57 ↗	12:28:13
0.0010	11354.40 ↗	12:28:11
0.0168	11354.97 ↗	12:28:11
0.0021	11354.60 ↗	12:28:10
0.0042	11354.44 ↗	12:28:09
0.1401	11353.76 ↘	12:28:09
0.1277	11354.05 ↘	12:28:08
0.0984	11354.06 ↘	12:28:08
0.0063	11354.69 ↗	12:28:08
0.0021	11353.28 ↗	12:28:07
0.0112	11353.28 ↗	12:28:06
0.0145	11353.28 ↗	12:28:06
0.0812	11353.60 ↘	12:28:05
0.2201	11354.00 ↘	12:28:05
0.0876	11354.72 ↗	12:28:05
0.0015	11354.75 ↘	12:28:05
0.0222	11357.92 ↗	12:28:04
0.0863	11357.93 ↗	12:28:03
0.0084	11357.78 ↗	12:28:01
0.1845	11357.20 ↘	12:28:01
0.1000	11357.21 ↘	12:28:01
0.0500	11357.36 ↘	12:28:01
0.0166	11357.37 ↘	12:28:01
0.0984	11357.80 ↘	12:28:01
0.0114	11358.36 ↗	12:28:01
0.4773	11356.66 ↘	12:27:59
0.0189	11356.85 ↘	12:27:59
0.1000	11357.03 ↘	12:27:59
0.0400	11358.02 ↘	12:27:59
0.0984	11358.03 ↘	12:27:59
0.0500	11358.28 ↘	12:27:59
0.0185	11359.08 ↘	12:27:59
0.0786	11359.11 ↘	12:27:59
0.0432	11359.12 ↗	12:27:56
0.0086	11359.11 ↘	12:27:53
0.0010	11359.33 ↗	12:27:52
0.0853	11359.32 ↗	12:27:52

Traditional Exchanges: Order Book Model

Order Book Based DEXs

Naive Approach:

- Implement an order book and matching engine on-chain.

Mostly unworkable with today's blockchains.

Order Book Based DEXs

Hybrid Approach — **The Relayer Model**

- Matching is done **off-chain** by a centralized “Relayer”
 - The relayer crafts a transaction off-chain that resembles an atomic-swap, then submits it to the blockchain
- Trade settlement is done on-chain

Many examples of DEXs that initially worked this way:

- ox protocol
- EtherDelta
- Kyber
- Airswap

Order Book Based DEXs

Limitations of the Relayer Model

- Peer-to-peer —hard to bootstrap liquidity
- Market making is expensive
- Depends on the presence of a centralized party
- Less programmable/composable

Great resource:

Front-Running, Griefing, and the Perils of Virtual Settlement,
by Will Warren

Is there a simpler way to build a DEX?

Two most important problems

- Complexity
- Bootstrapping liquidity

Desired Characteristics

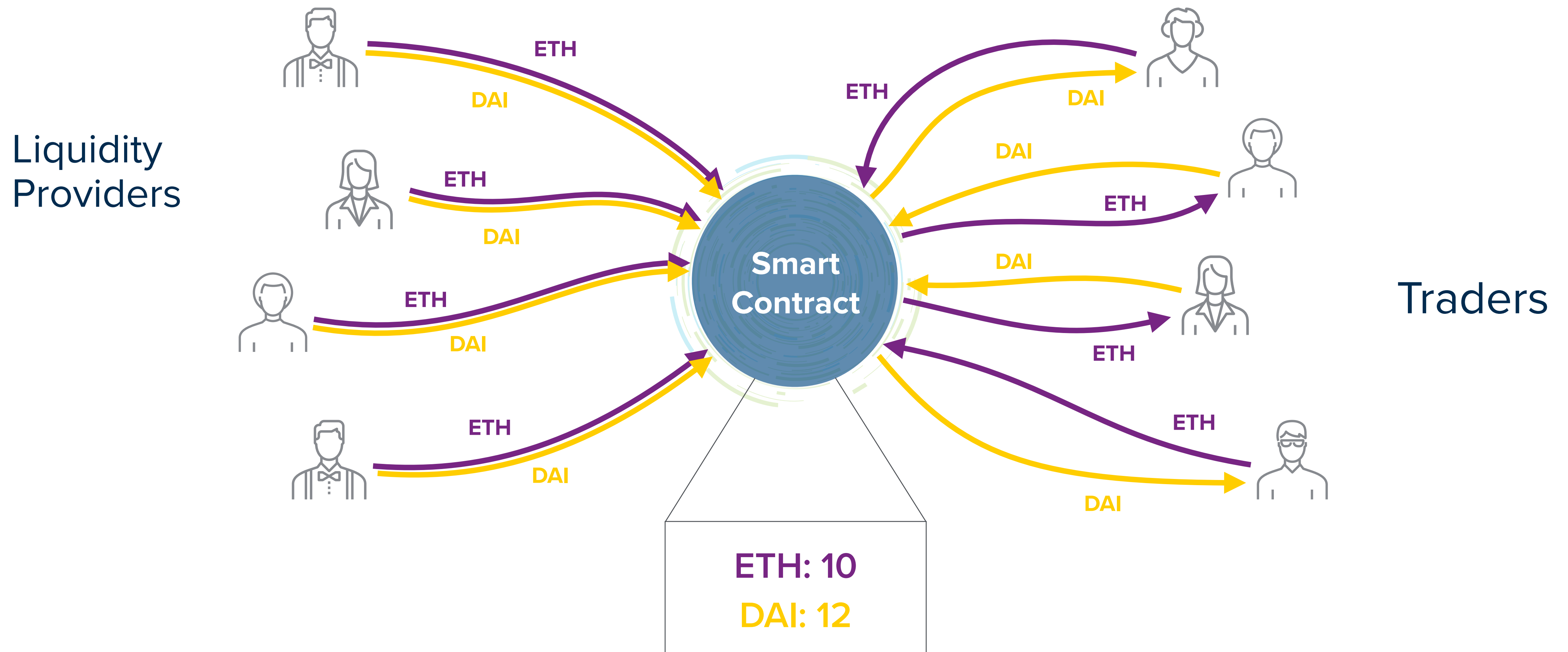
- Simple — buildable as a smart contract
- Automated liquidity — no dependence on active market-makers
- No single points of control — no dependence on centralized parties

A Bit of History: Automated Market Makers (AMMs)

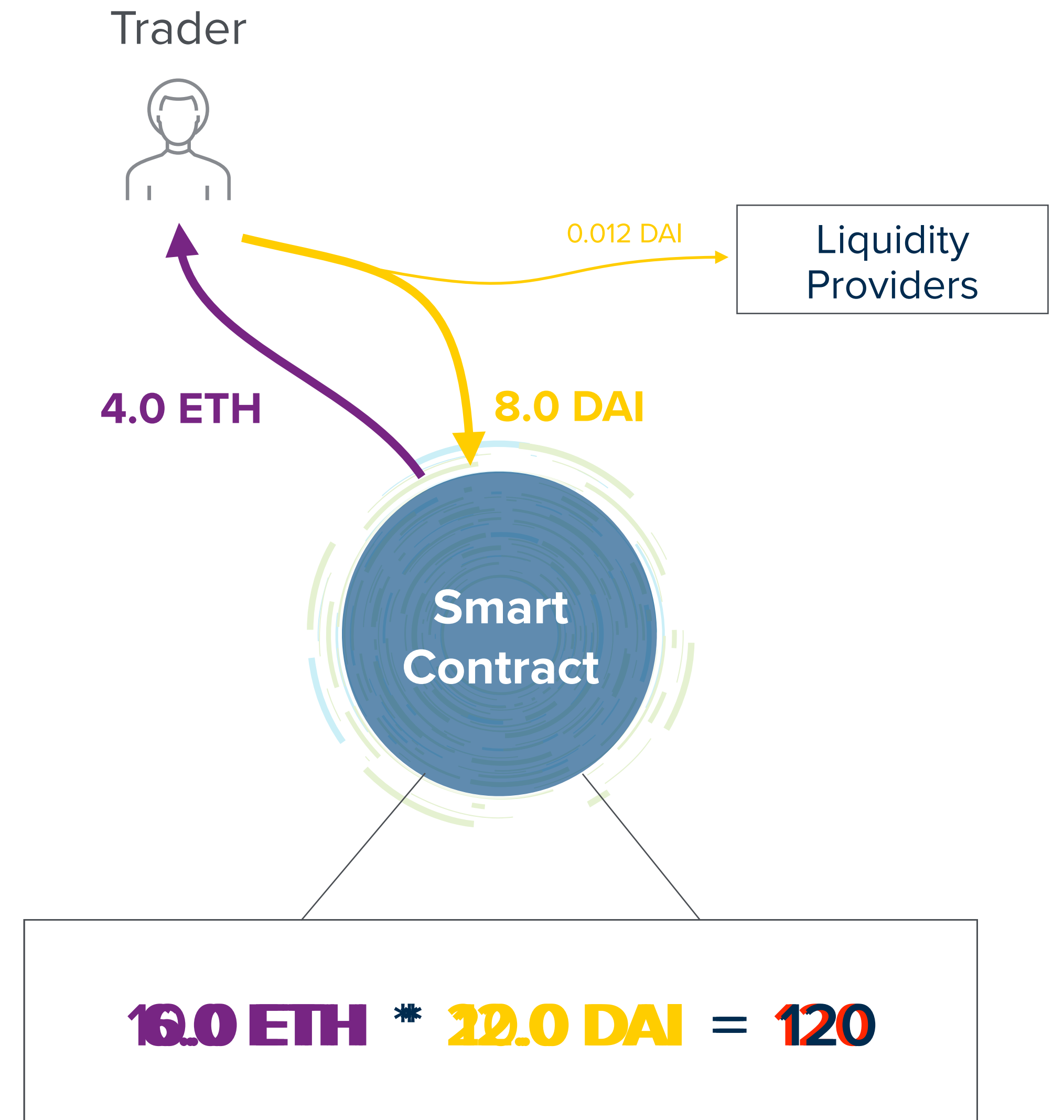
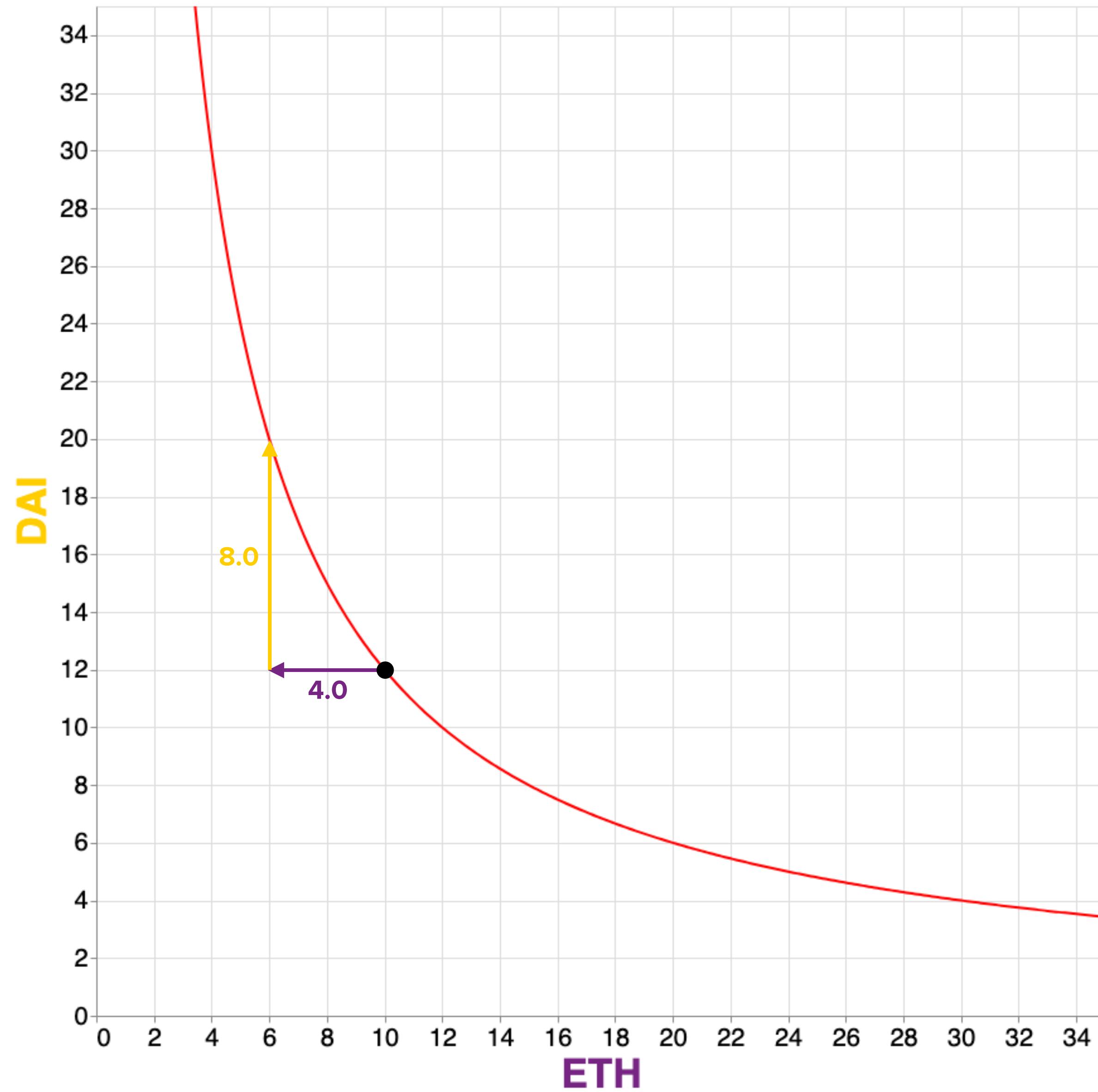
- Pricing shares in prediction markets —
Hanson's Market Scoring Rules
 - Also used to price online ads
- Idea first explored in crypto in 2016 by:
 - Vitalik Buterin — reddit post
- Then generalized by Alan Lu and Martin Koppelman:
 - Blogpost: Building a Decentralized Exchange in Ethereum

High Level Aspiration

Two-Sided Marketplace



$$xy = k$$



Invariant: k

Simple Pricing Rule

$$(x - \Delta x)(y + \Delta y) = k$$



$$xy = k$$

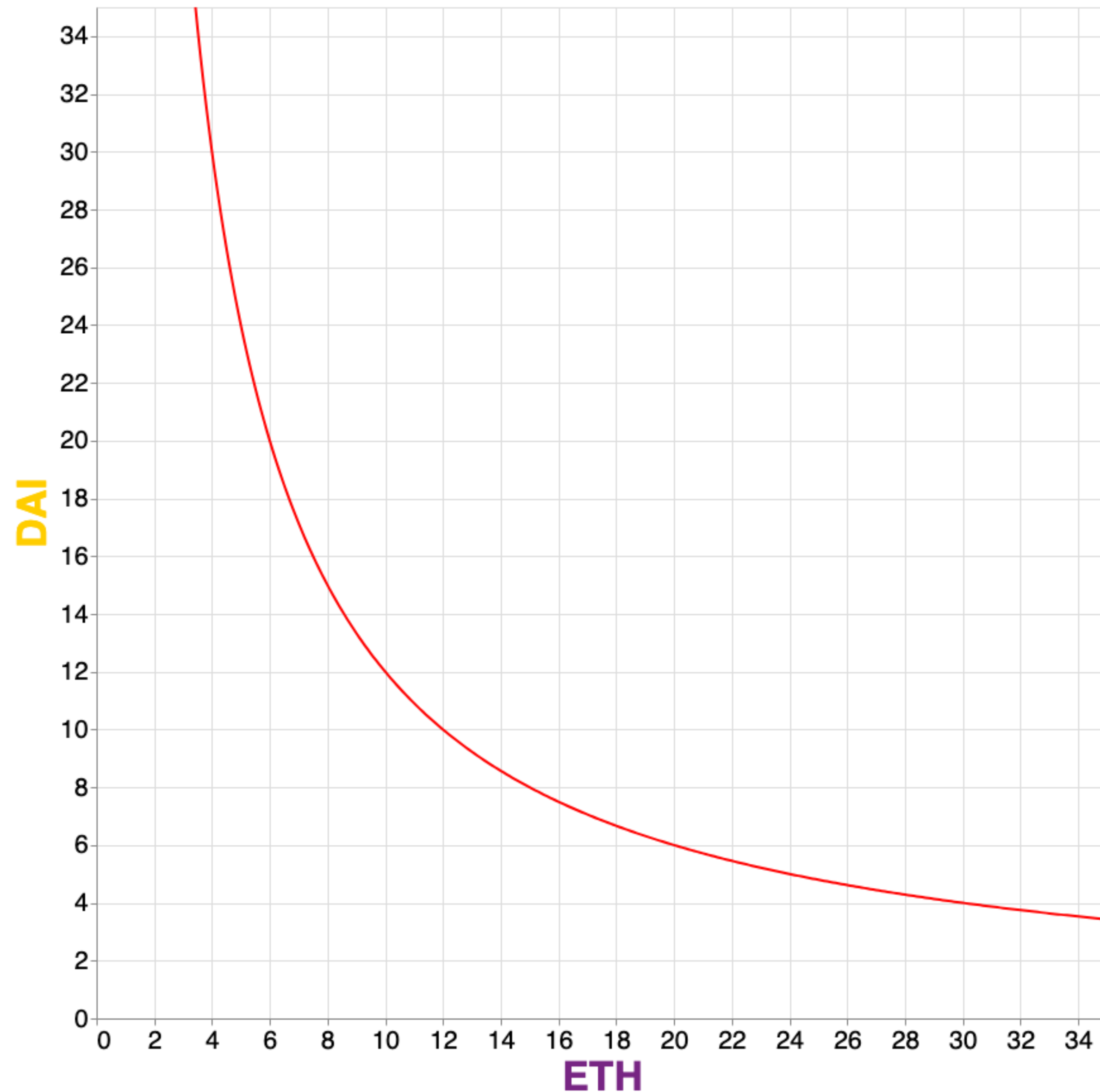
Simple Pricing Rule

$$(x - \Delta x)(y + \phi \Delta y) = k$$

where $(1 - \phi)$ is the percentage fee that is paid to liquidity providers, and where $\Delta x > 0$ and $\Delta y > 0$.



$$xy = k$$



Simple Pricing Rule

$$(x - \Delta x)(y + \phi \Delta y) = k$$

$$\begin{aligned} \phi \Delta y &= \frac{xy}{x - \Delta x} - y \\ &= \frac{xy - y(x - \Delta x)}{x - \Delta x} \\ &= \frac{\cancel{xy} - \cancel{xy} - y\Delta x}{x - \Delta x} \end{aligned}$$

$$\Delta y = \frac{1}{\phi} \cdot \frac{y\Delta x}{x - \Delta x}$$

$$xy = k$$



Simple Pricing Rule

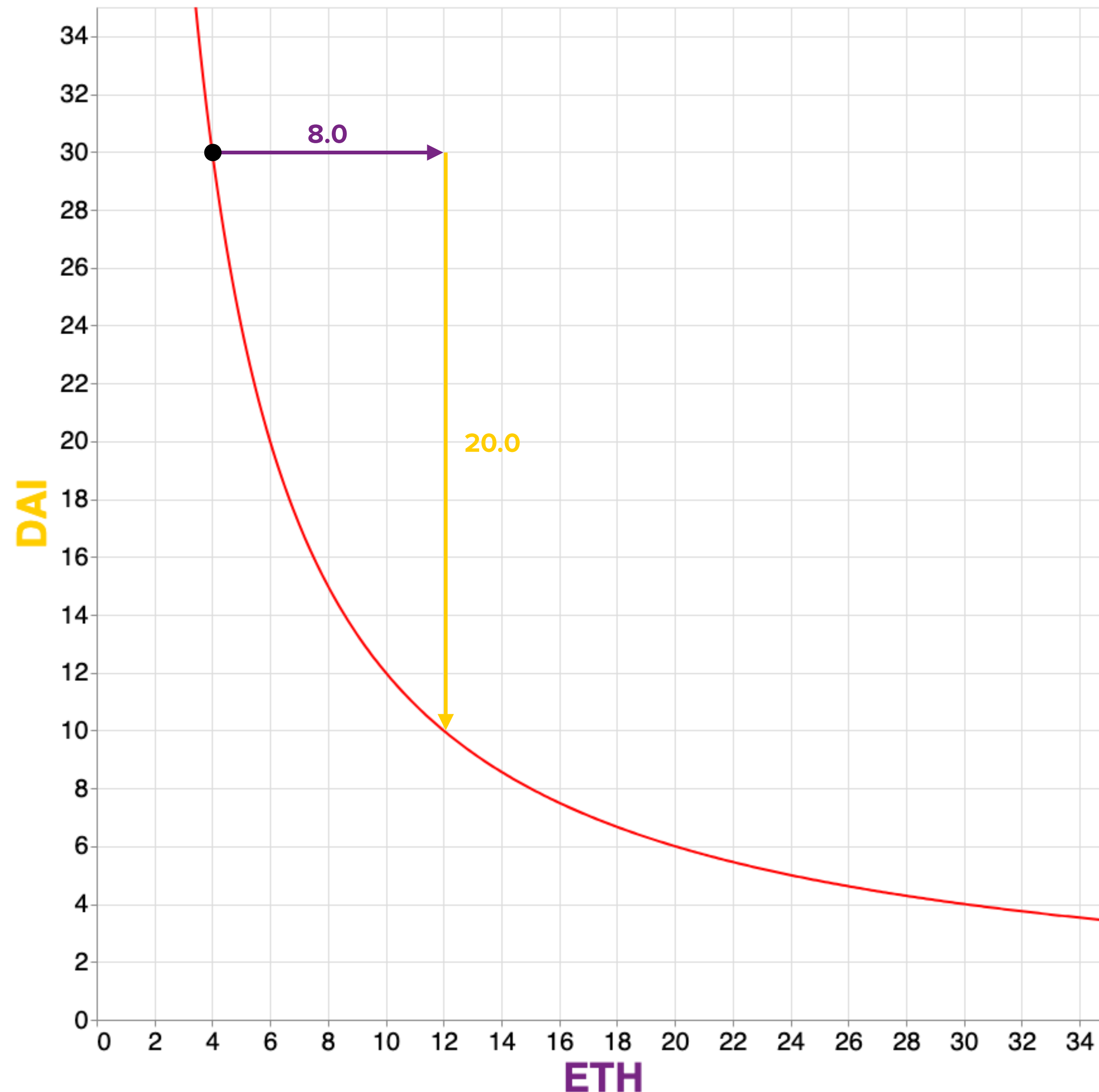
$$\Delta y = \frac{1}{\phi} \cdot \frac{y\Delta x}{x - \Delta x}$$

This rule specifies the price of *buying* Δx in terms of y .

A similar exercise (swapping x s and y s) produces a rule that specifies the price of *selling* Δx in terms of y :

$$\Delta y = \frac{y\phi\Delta x}{x + \phi\Delta x}$$

$$xy = k$$



Simple Pricing Rule

Example where the contract contains **4.0 ETH** and **30.0 DAI** and charges a fee for liquidity providers of 30 bps.

$$\Delta y = \frac{y\phi\Delta x}{x + \phi\Delta x}$$

$$\Delta y = \frac{30 * 0.997 * \Delta x}{4 + 0.997 * \Delta x}$$

Say a trader wants to *sell* **8.0 ETH** to the contract. How much **DAI** should she get in return?

$$\Delta y = \frac{30 * 0.997 * 8}{4 + 0.997 * 8} = 19.98$$

(The fee to liquidity providers is 0.02.)

In the Wild: Uniswap

Selling x for y

$$\Delta y = \frac{y\phi\Delta x}{x + \phi\Delta x}$$

Buying x for y

$$\Delta y = \frac{1}{\phi} \cdot \frac{y\Delta x}{x - \Delta x}$$

```
41
42 // given an input amount of an asset and pair reserves, returns the maximum output amount of the other asset
43 function getAmountOut(uint amountIn, uint reserveIn, uint reserveOut) internal pure returns (uint amountOut) {
44     require(amountIn > 0, 'UniswapV2Library: INSUFFICIENT_INPUT_AMOUNT');
45     require(reserveIn > 0 && reserveOut > 0, 'UniswapV2Library: INSUFFICIENT_LIQUIDITY');
46     uint amountInWithFee = amountIn.mul(997);
47     uint numerator = amountInWithFee.mul(reserveOut);
48     uint denominator = reserveIn.mul(1000).add(amountInWithFee);
49     amountOut = numerator / denominator;
50 }
51
```

```
51
52 // given an output amount of an asset and pair reserves, returns a required input amount of the other asset
53 function getAmountIn(uint amountOut, uint reserveIn, uint reserveOut) internal pure returns (uint amountIn) {
54     require(amountOut > 0, 'UniswapV2Library: INSUFFICIENT_OUTPUT_AMOUNT');
55     require(reserveIn > 0 && reserveOut > 0, 'UniswapV2Library: INSUFFICIENT_LIQUIDITY');
56     uint numerator = reserveIn.mul(amountOut).mul(1000);
57     uint denominator = reserveOut.sub(amountOut).mul(997);
58     amountIn = (numerator / denominator).add(1);
59 }
60
```

UniswapV2Library.sol

[Swap](#)[Pool](#)[UNI](#)[Vote](#)[Charts[↗]](#)

0 UNI

1.39 ETH

0×28E9...1E88 



From

Balance: 1.39092

0.0

MAX

 ETH

▼

↓

To

-

0.0

Select a token

▼

Enter an amount

Quick Demo: <https://app.uniswap.org/>

How to Think about an AMM's Price

Price is the ratio between assets (e.g. **DAI**) paid and assets (e.g. **ETH**) received.

If I pay **100 DAI** for **4 ETH**, then my price per ETH is 25 DAI.

In our notation, this is given by $\Delta y / \Delta x$.

Selling x for y

$$\Delta y = \frac{y\phi\Delta x}{x + \phi\Delta x}$$

Buying x for y

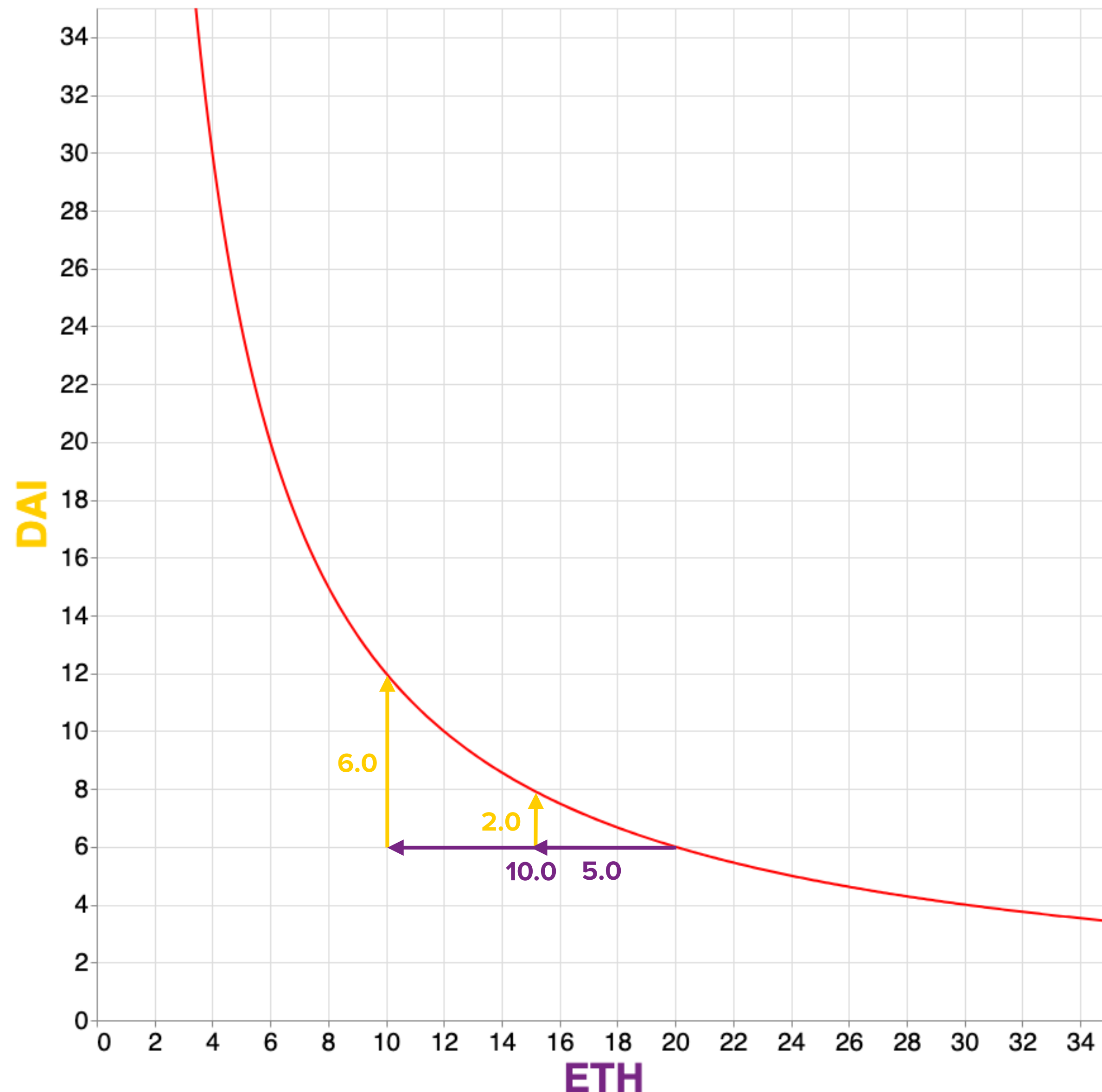
$$\Delta y = \frac{1}{\phi} \cdot \frac{y\Delta x}{x - \Delta x}$$

Divide both sides by Δx to get $\Delta y / \Delta x$.

$$\frac{\Delta y}{\Delta x} = \frac{y\phi}{x + \phi\Delta x}$$

$$\frac{\Delta y}{\Delta x} = \frac{1}{\phi} \cdot \frac{y}{x - \Delta x}$$

$$xy = k$$



Marginal Price & Slippage

Selling x for y

$$\frac{\Delta y}{\Delta x} = \frac{y\phi}{x + \phi\Delta x}$$

Buying x for y

$$\frac{\Delta y}{\Delta x} = \frac{1}{\phi} \cdot \frac{y}{x - \Delta x}$$

Observation #1

Pricing depends on the size of the trade, Δx .

For example with **20.0 ETH** * **6.0 DAI** = **120**,

Buying **10 ETH** (i.e. $\Delta x = 10$) costs 6.02 DAI*

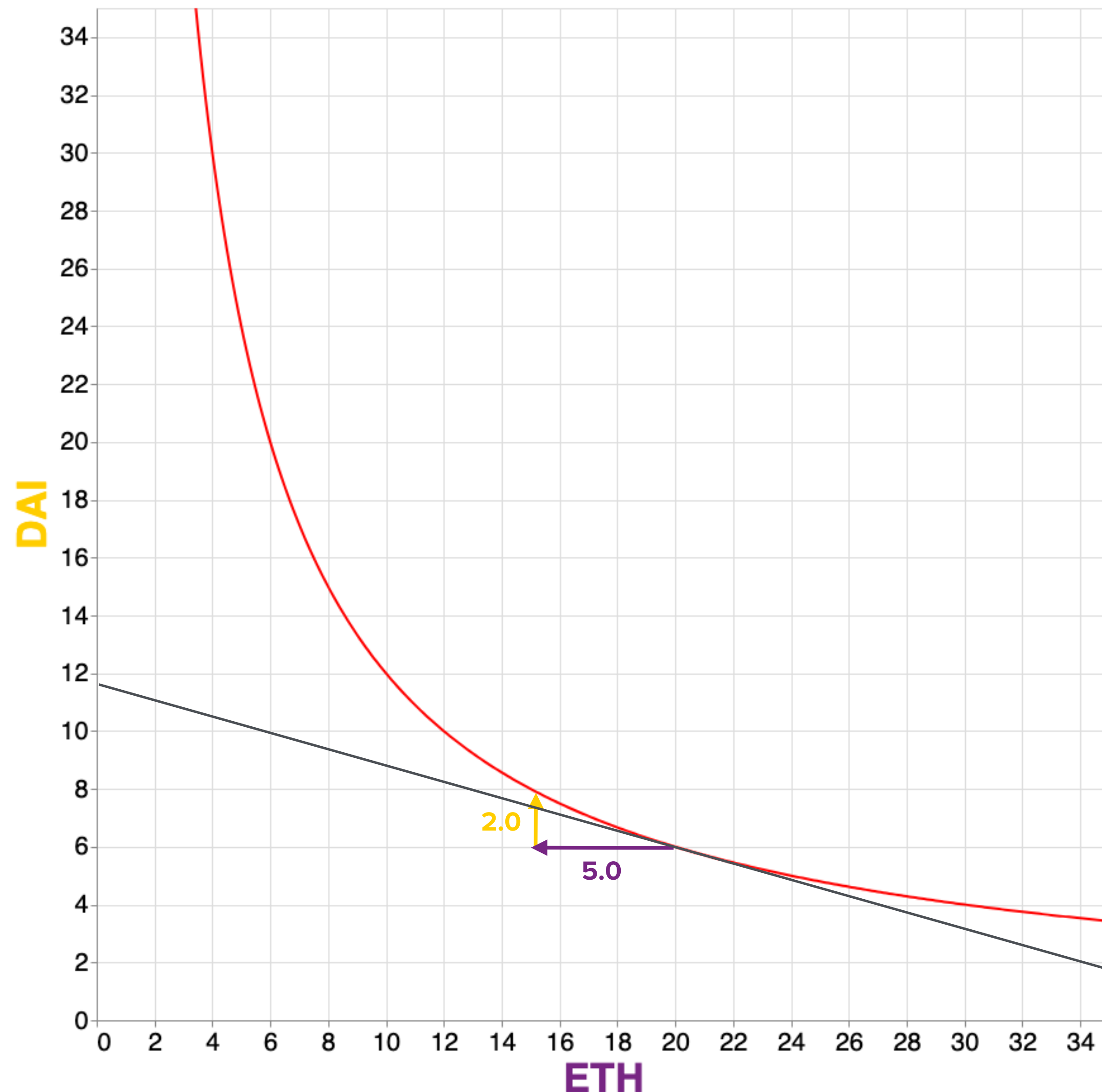
Or **0.602 DAI** per ETH

Whereas buying **5 ETH** costs 2.006 DAI

Or **0.401 DAI** per ETH

* assuming $\phi = 0.997$

$$xy = k$$



Marginal Price & Slippage

Selling x for y

$$\frac{\Delta y}{\Delta x} = \frac{y\phi}{x + \phi\Delta x}$$

Buying x for y

$$\frac{\Delta y}{\Delta x} = \frac{1}{\phi} \cdot \frac{y}{x - \Delta x}$$

In the limit, as Δx approaches 0:

$$\lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x} = \phi \frac{y}{x}$$

$$\lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x} = \frac{1}{\phi} \frac{y}{x}$$

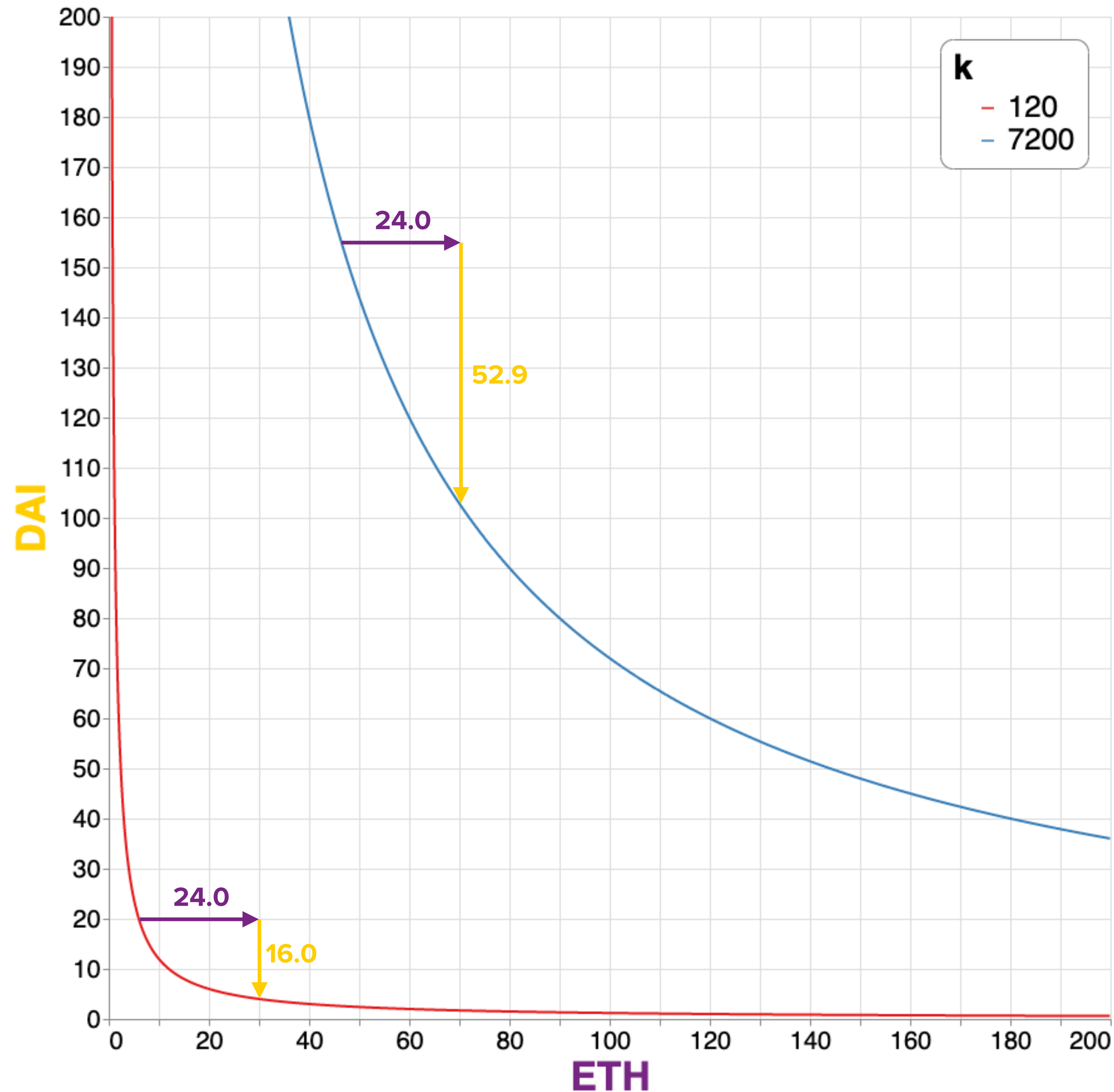
And, if we set the fee to zero ($\phi = 1$), then:

$$M_p = \frac{y}{x}$$

where M_p denotes
marginal price

M_p is equal to the slope of the tangent line.

$$xy = k$$



Marginal Price & Slippage

Selling x for y

$$\frac{\Delta y}{\Delta x} = \frac{y\phi}{x + \phi\Delta x}$$

Buying x for y

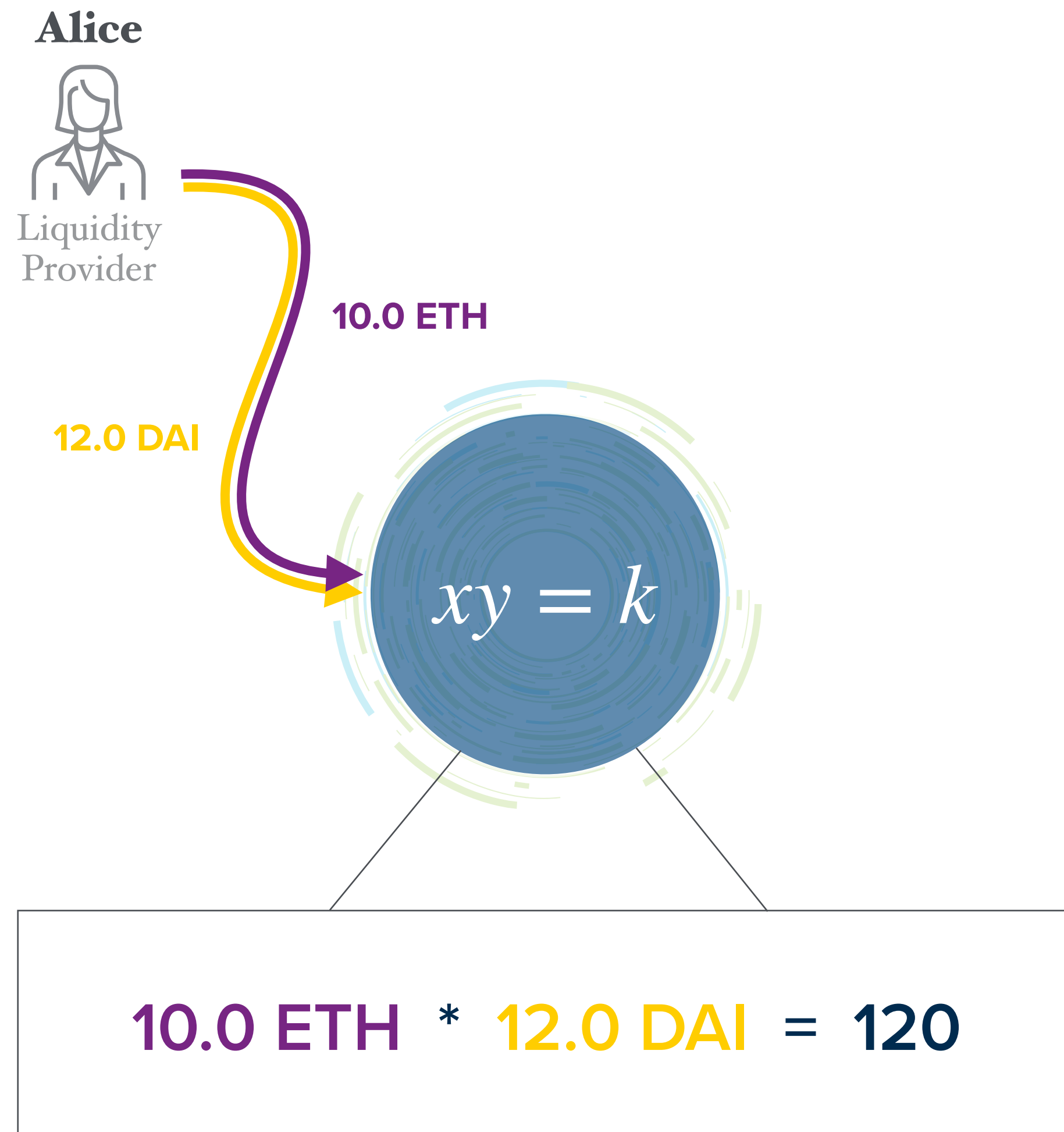
$$\frac{\Delta y}{\Delta x} = \frac{1}{\phi} \cdot \frac{y}{x - \Delta x}$$

Observation #2

Pricing depends on the size of x and y (i.e. k)

It's straightforward to see that, as k increases, the effective price of the AMM is less sensitive to Δx .

Incentives for Liquidity Providers



Alice deposits 10 ETH and 12 DAI of liquidity, which implies:

$$M_p = 1.2 \quad \text{where } M_p \text{ denotes } \textit{marginal price}$$

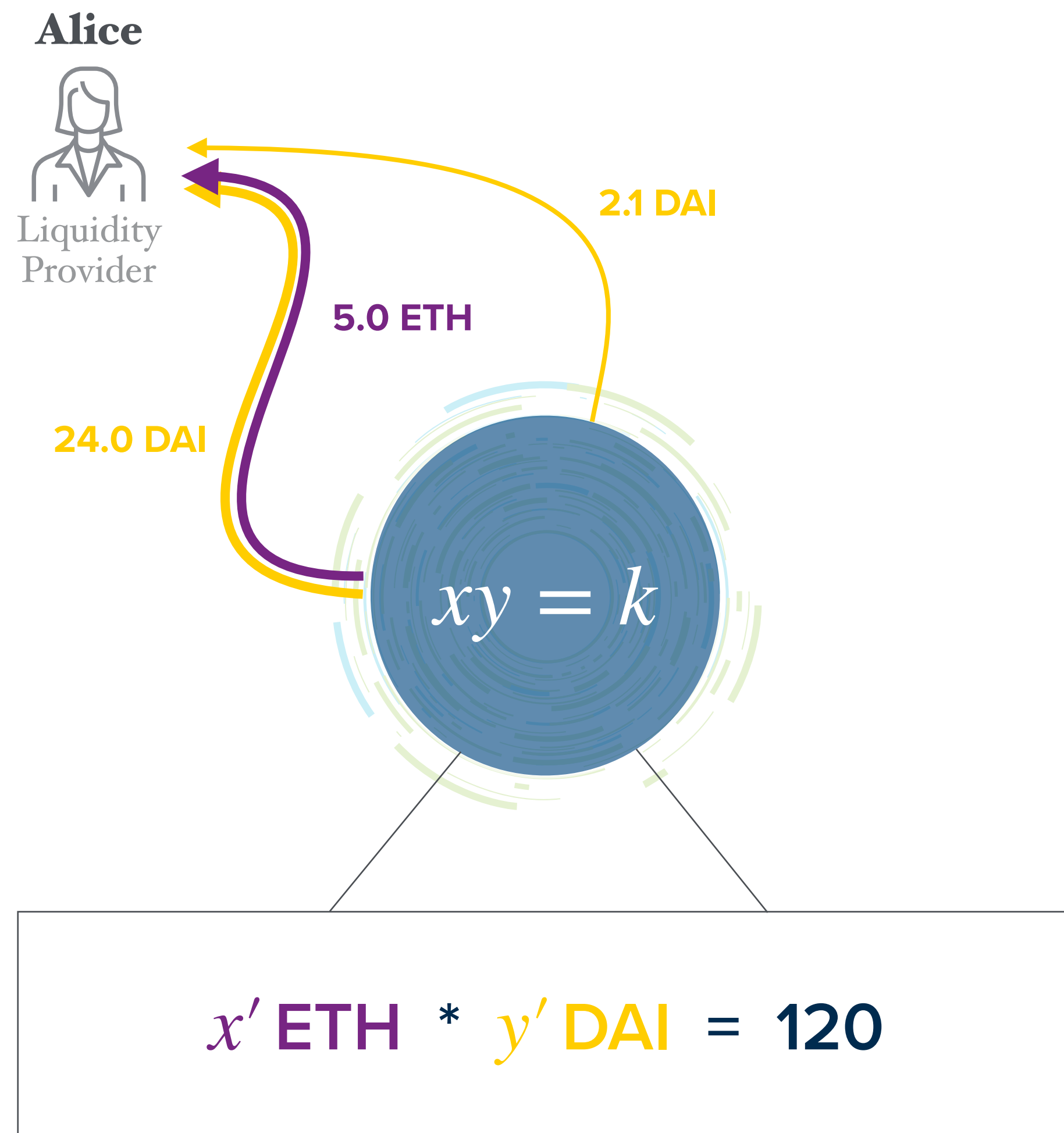
Alice waits for a month, during which traders drive \$700 worth of volume through the AMM.

At the end of the month, Alice withdraws her ETH and DAI. By that time, the price of ETH has gone up 4x. The marginal price is now:

$$M'_p = 4.8$$

What is Alice's return?

Assume: $(1 - \phi) = 0.003$

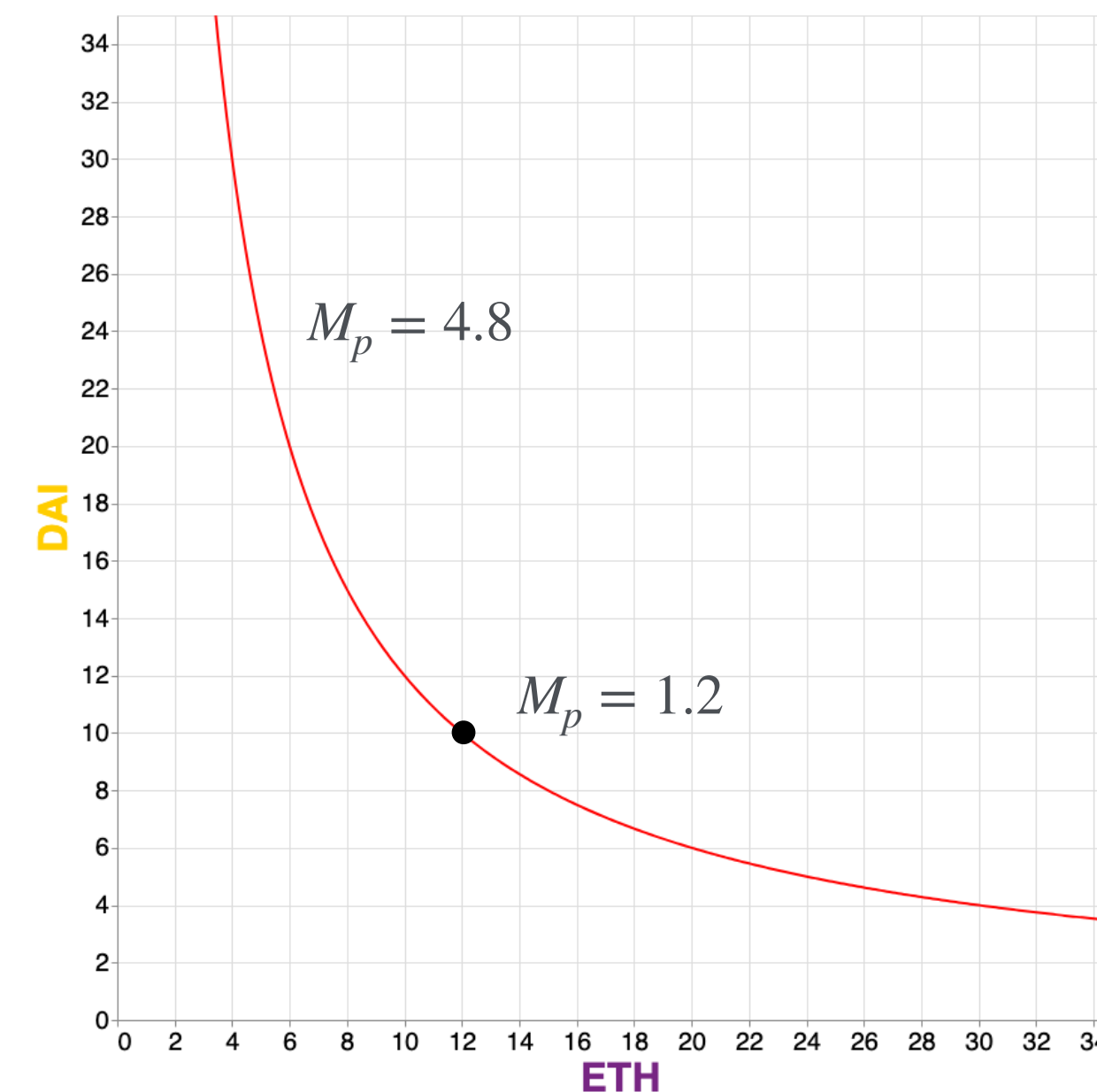


First, what does Alice earn from liquidity provider fees?

$$V(1 - \phi) = 700 * 0.003 = \$2.1$$

where V denotes trading volume

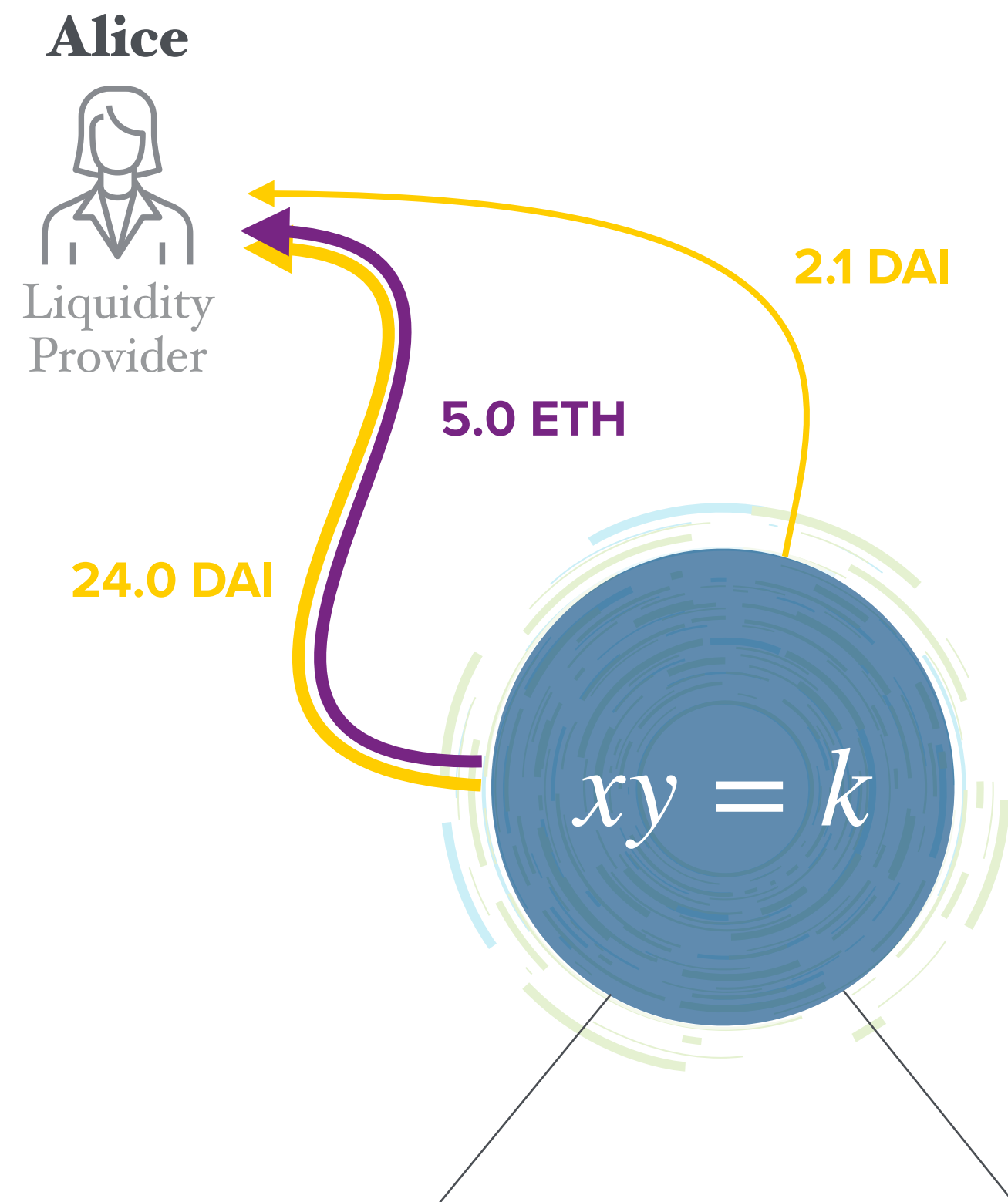
Second, how many ETH and DAI does Alice get back?



$$x' = 5 \text{ ETH}$$

$$y' = 24 \text{ DAI}$$

Impermanent Divergence Loss



$$x' \text{ ETH} * y' \text{ DAI} = 120$$

So, how did Alice do?

Measured in DAI, Alice now has:

$$R = 5 \text{ ETH} * \frac{4.8 \text{ ETH}}{\text{DAI}} + 24 \text{ DAI} + 2.1 \text{ DAI}$$

$$R = 50.1 \text{ DAI}$$

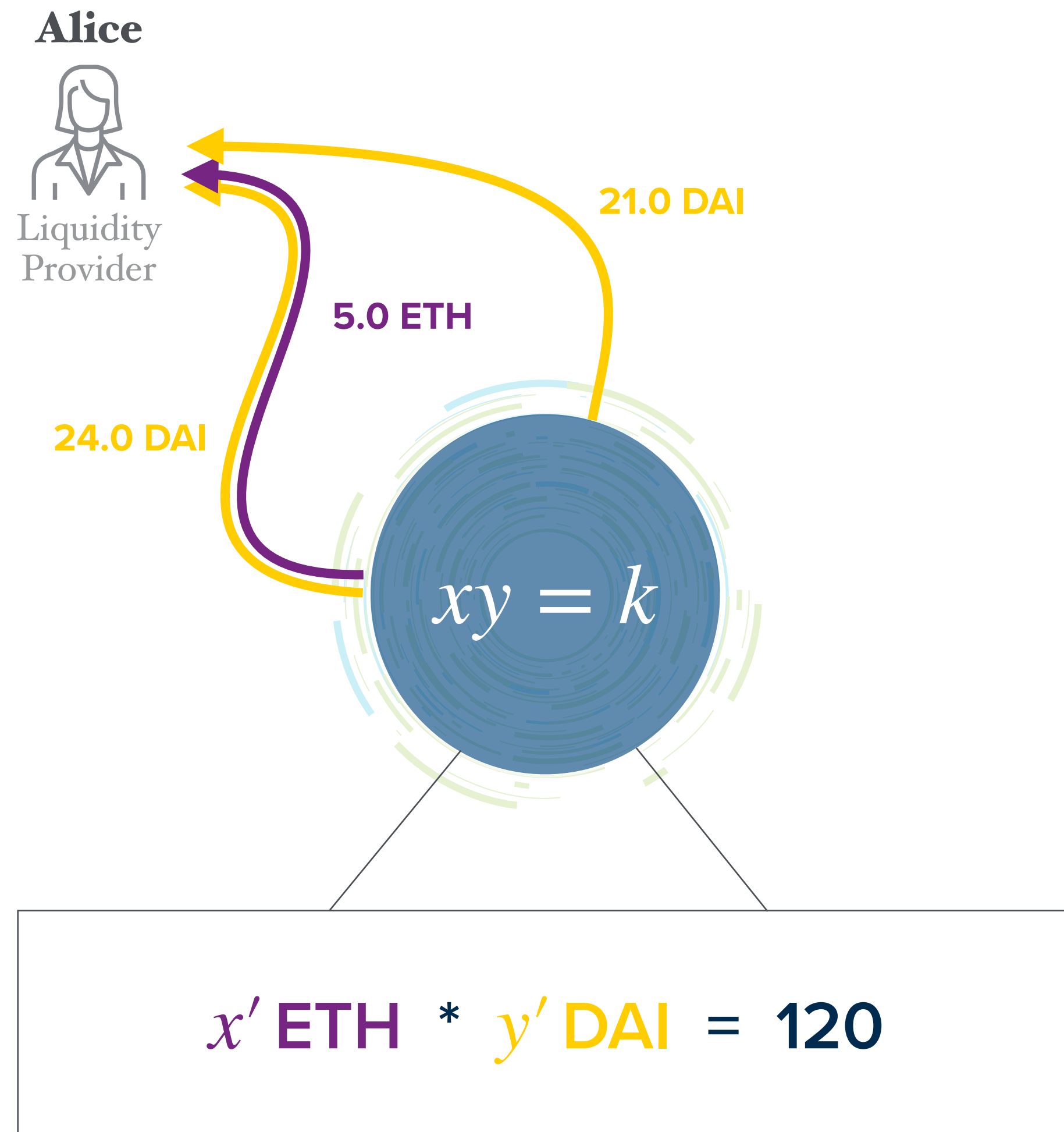
Not bad, but how would she have done if she had just held onto her 12 ETH and 10 DAI?

$$R_B = 12 \text{ ETH} * \frac{4.8 \text{ ETH}}{\text{DAI}} + 10 \text{ DAI}$$

$$R_B = 67.6 \text{ DAI}$$

This is called ~~impermanent~~ loss divergence

Impermanent Divergence Loss



What if volume had been higher?

Say, volume had been \$7,000 instead of \$700:

$$V(1 - \phi) = 7000 * 0.003 = \$21$$

Therefore,

$$R = 5 \text{ ETH} * \frac{4.8 \text{ ETH}}{\text{DAI}} + 24 \text{ DAI} + 21 \text{ DAI}$$

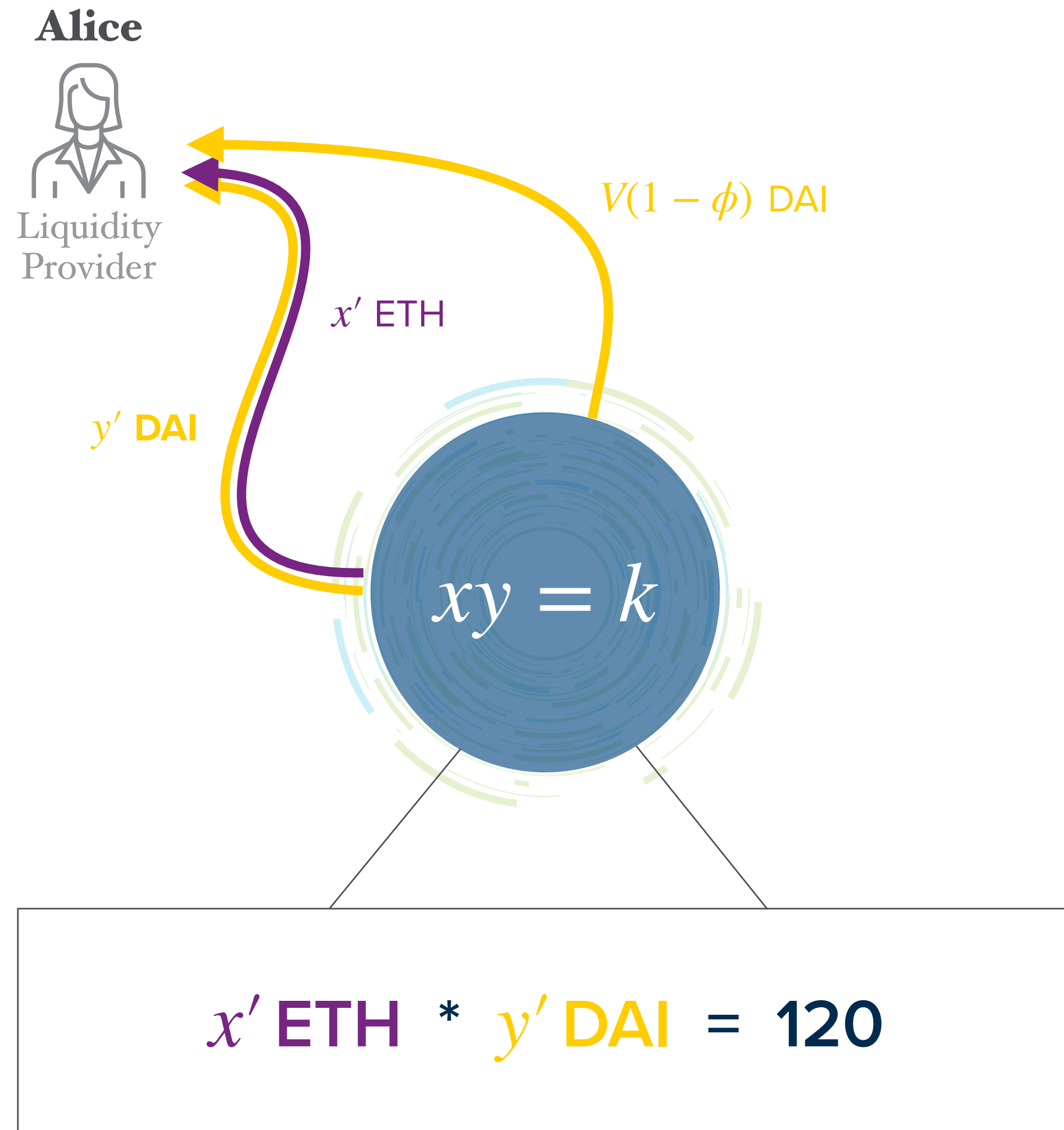
$$R = 69.0 \text{ DAI}$$

This time, Alice's returns are greater than her baseline return R_B of 67.6 DAI. Her profit:

$$P_L = \frac{R}{R_B} - 1 = 2.1 \%$$

Impermanent Divergence Loss

More generally



Alice's return R is given by:

$$R = x'M'_p + y' + V(1 - \phi)$$

Her baseline return R_B is given by:

$$R_B = xM_p + y$$

Her profit, in percentage terms is given by:

$$P_L = \frac{R}{R_B} - 1 = \frac{x'M'_p + y' + V(1 - \phi)}{xM_p + y} - 1$$

Let's ignore the volume term for now, and simplify:

$$P_L = \frac{x'M'_p + y'}{xM_p + y} - 1 \quad \text{assuming } V = 0 \text{ for now}$$

Recall

$$xy = k \quad \text{and} \quad M_p = y/x$$

Thus,

$$x = \sqrt{\frac{k}{M_p}} \quad \text{and} \quad y = \sqrt{kM_p}$$

Also,

$$x' = \sqrt{\frac{k}{M'_p}} \quad \text{and} \quad y' = \sqrt{kM'_p}$$

Finally, let:

$$M'_p = rM_p$$

Impermanent Divergence Loss

Simplifying

$$P_L = \frac{x'M'_p + y'}{xM_p + y}$$

Step 1: let's express everything in terms of M_p and k .

$$P_L = \frac{\sqrt{\frac{k}{rM_p}}rM_p + \sqrt{krM_p}}{\sqrt{\frac{k}{M_p}}rM_p + \sqrt{kM_p}} - 1 = \frac{2\sqrt{r}\cancel{\sqrt{kM_p}}}{r\cancel{\sqrt{kM_p}} + \cancel{\sqrt{kM_p}}} - 1$$

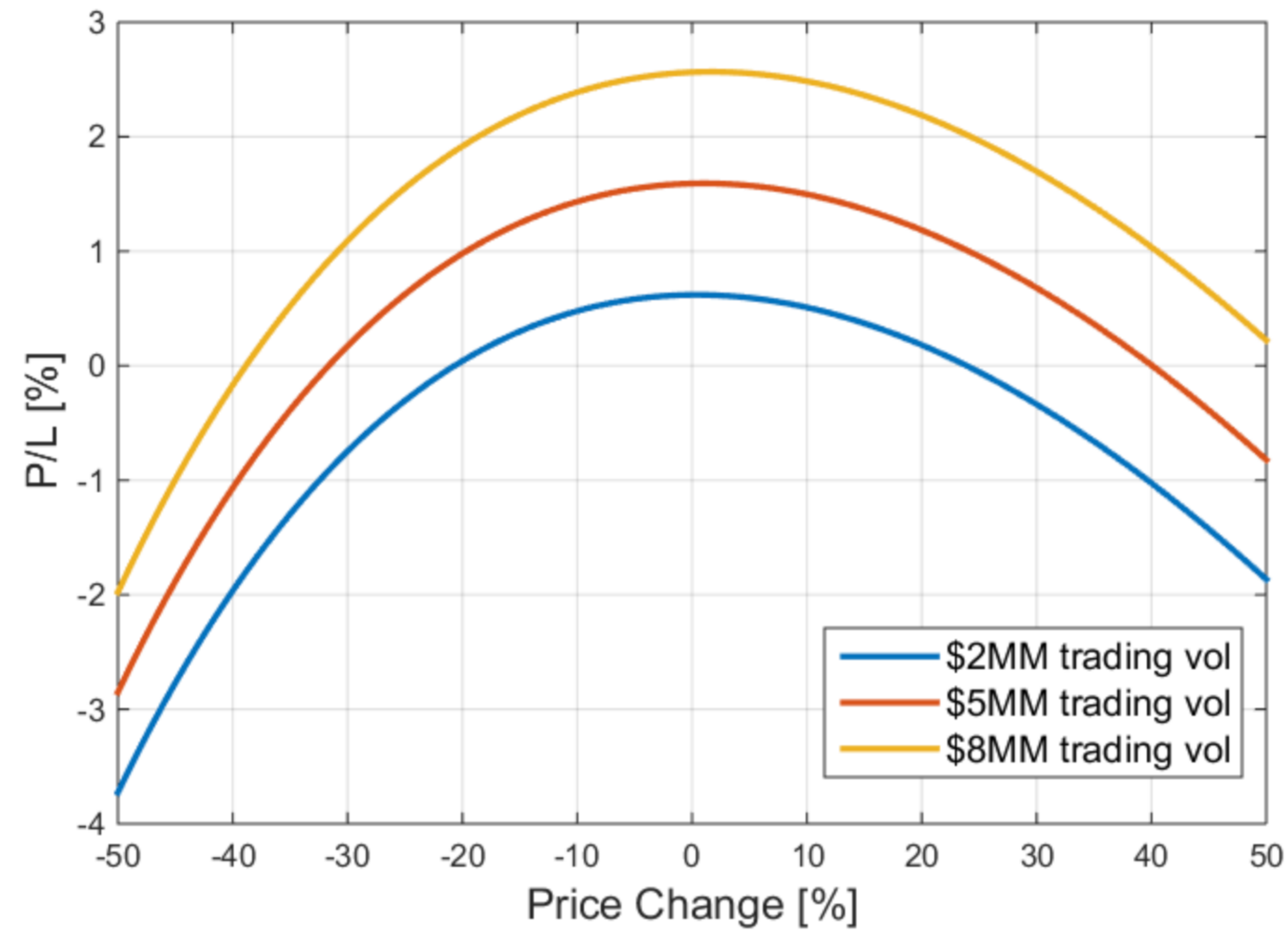
$$P_L = \frac{2\sqrt{r}}{r + 1} - 1$$

Step 2: Reintroduce the volume term:

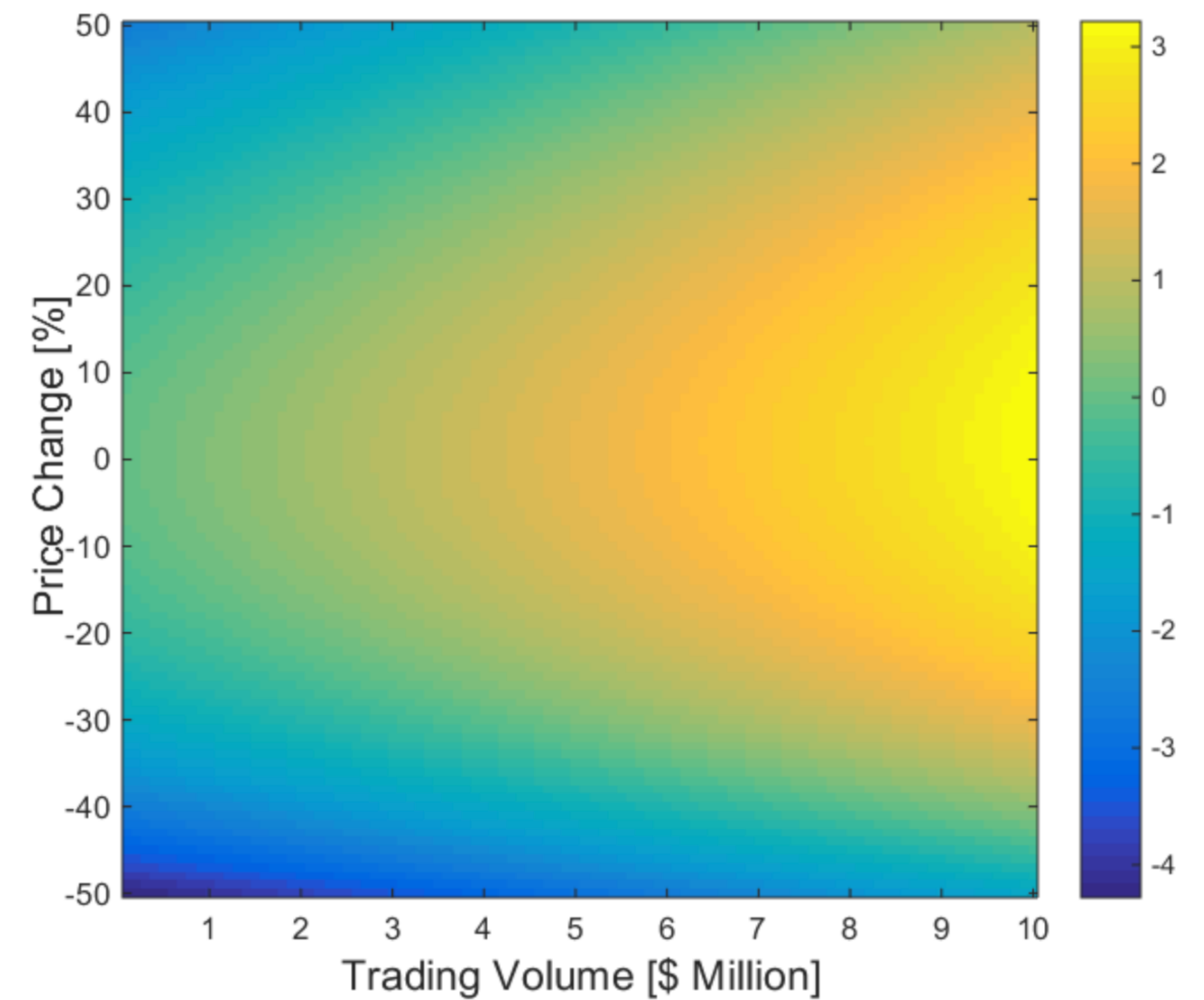
$$P_L = \frac{2\sqrt{r}}{r + 1} + \frac{V(1 - \phi)}{c} - 1$$

Step 3: Plot this equation

Impermanent Divergence Loss



Optimal P/L occurs when the final price is equal to that at liquidity provisioning



P/L percentage of liquidity provision on Uniswap for different scenarios of exchange trading volume and ETH price change

$$P_L = \frac{2\sqrt{r}}{r+1} + \frac{V(1-\phi)}{c} - 1$$

Uniswap ROI By Token

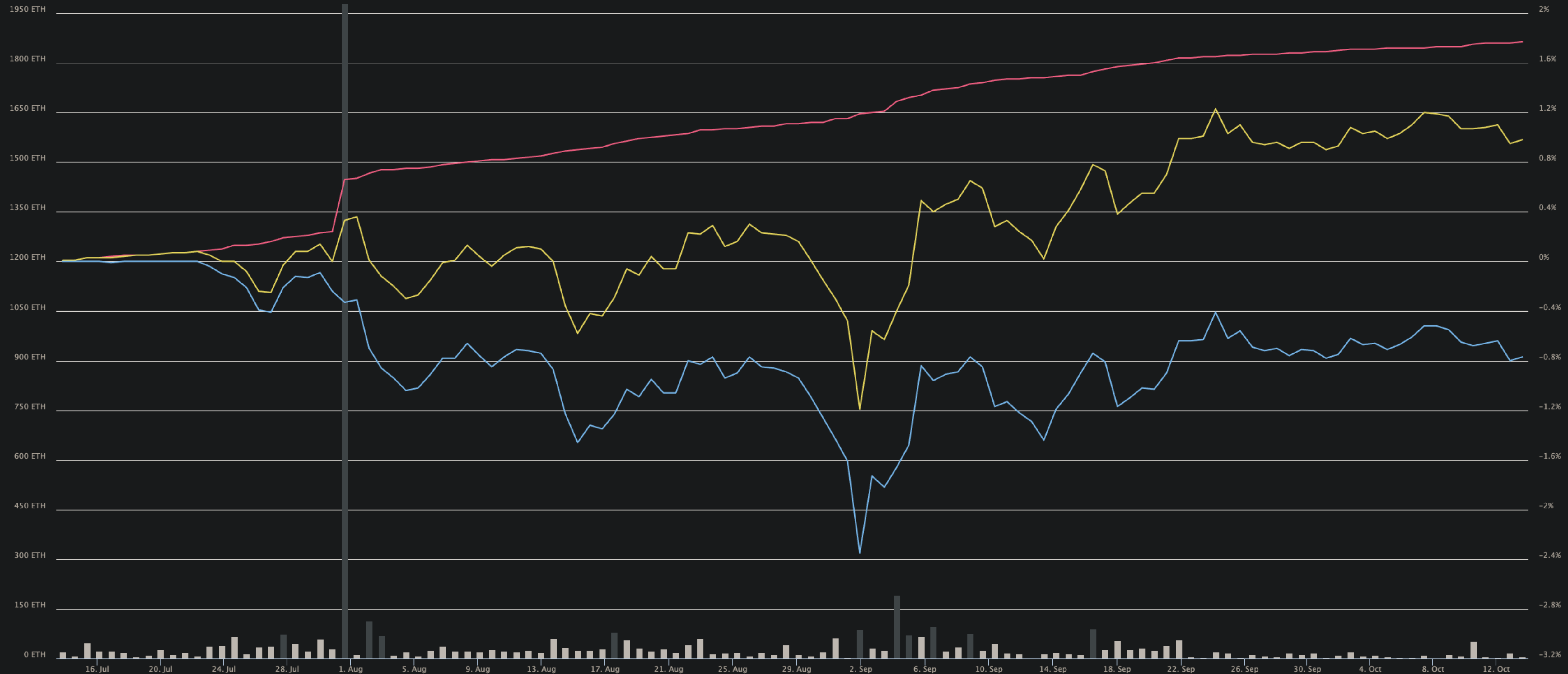
WBTC ▾

Quick Demo: <https://zumzoom.github.io/analytics/uniswap/roi/>

📘 Hodl 50/50 ▾

Zoom 1w 1m 1m 6m 1y All

From Jul 13, 2020 To Oct 13, 2020



Uniswap's Metrics To Date

ETH Price: \$380.63 Transactions (24H): 161,342 Pairs: 14,974 Fees (24H): \$612,220

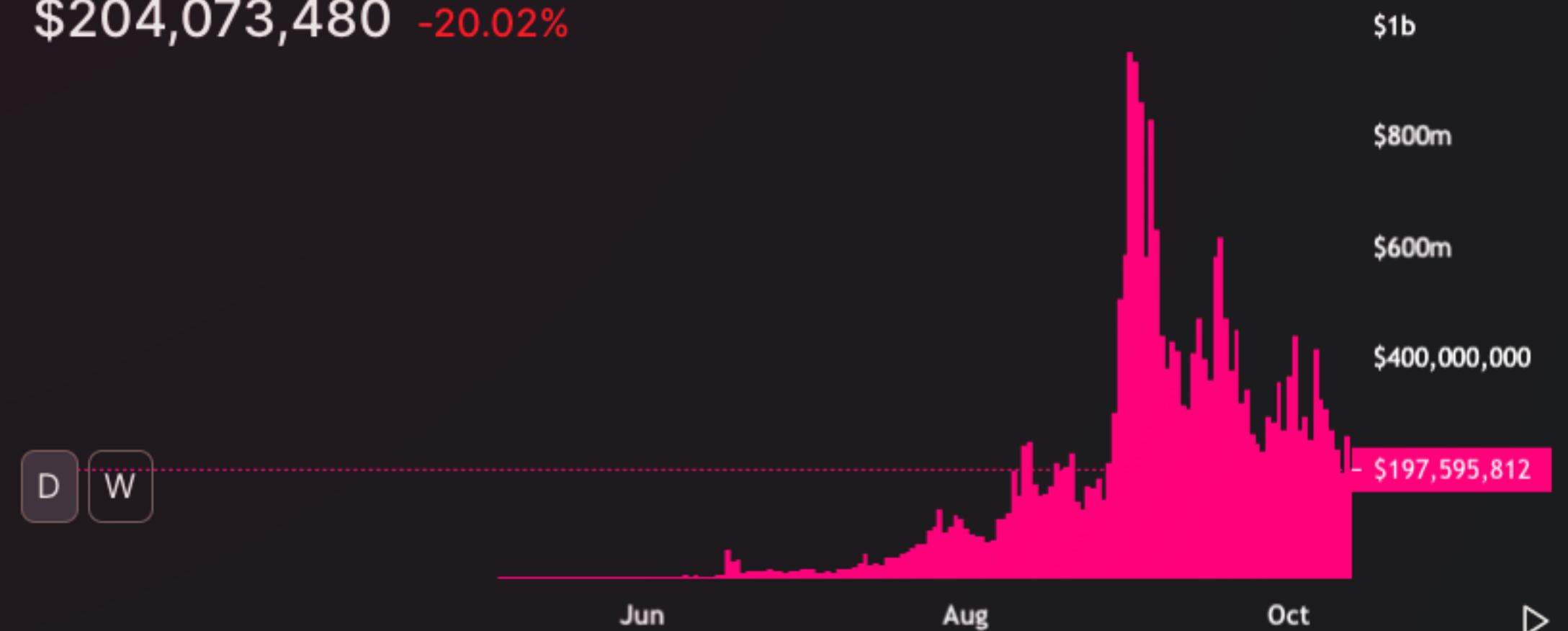
Liquidity

\$2.87b -1.61%



Volume (24hr)

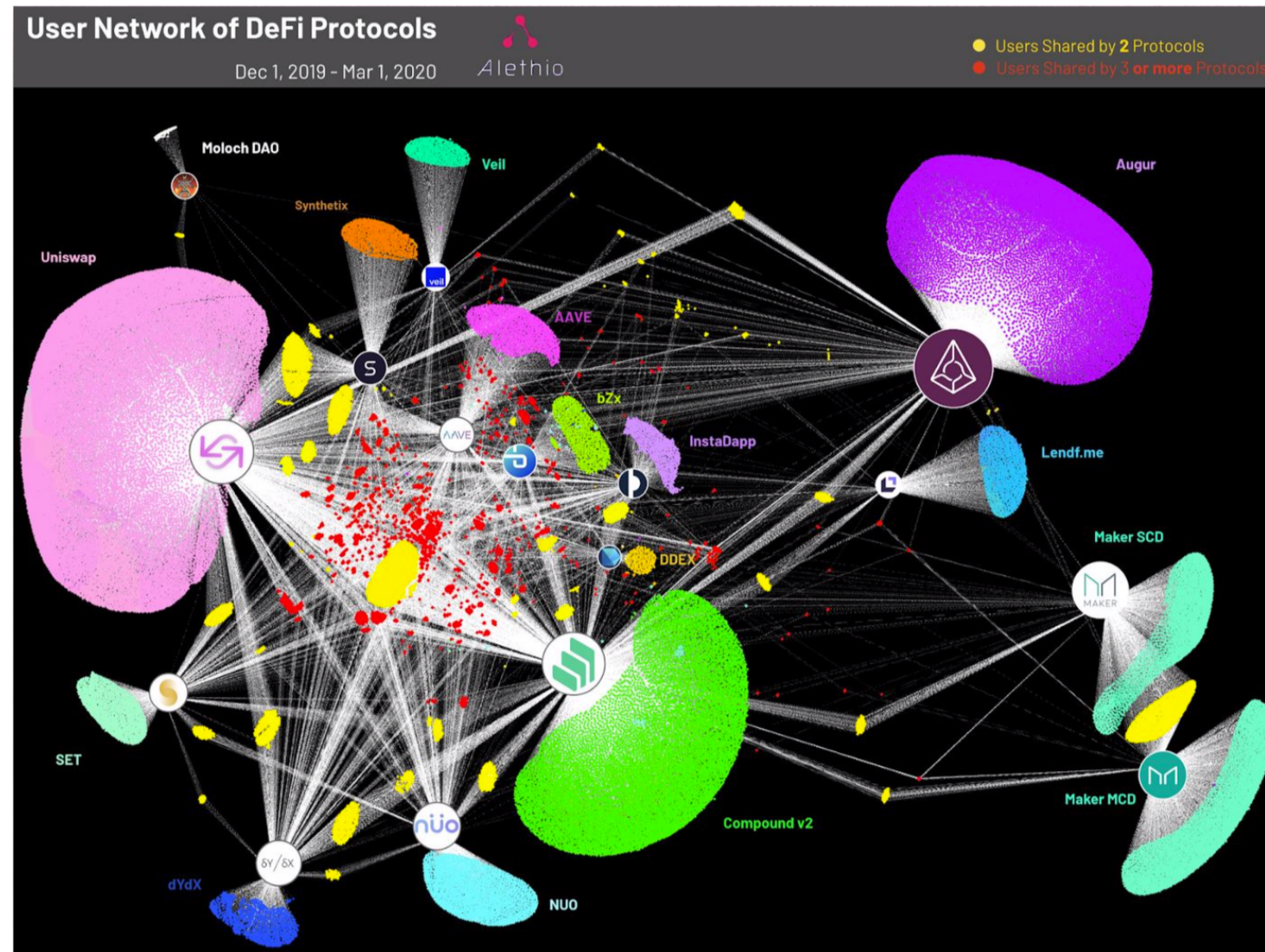
\$204,073,480 -20.02%



Quick Demo: <https://uniswap.info/>

Example: Uniswap

Interoperability



Optional: Generalizations of $xy = k$

- Curve: <https://www.curve.fi/>
- Balancer: <https://balancer.finance/>

DEXs: Concluding Thoughts

Desired Characteristics

- Simple — buildable as a smart contract
- Automated liquidity — no dependence on active market-makers
- No single points of control

Decentralized Lending

Eddy Lazzarin

Overcollateralized
vs
Undercollateralized

Centralized Lending

Example: Overcollateralized Margin Trading

- Trust the exchange not to get hacked, steal assets, or incorrectly calculate balances
- Borrowed assets only exist on the exchange: they can't be used on the blockchain (no protocol composability)
- Interest payments go to the exchange

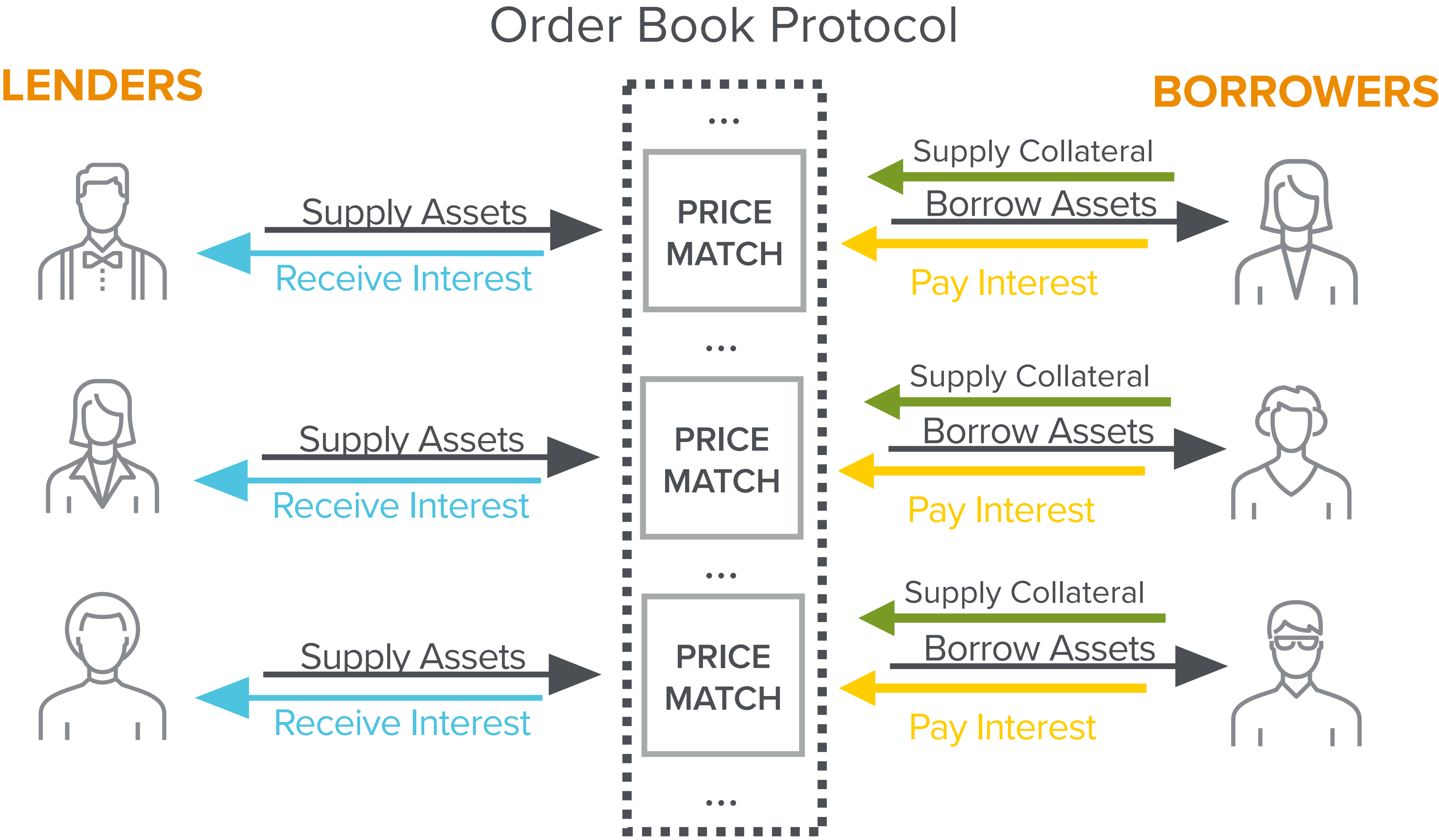
Decentralized Lending

High Level Motivation

- Minimize trust required in the counter-party
- Borrowed assets can be used freely on the blockchain (enable protocol composability)
- Interest payments go from asset borrowers to asset suppliers, neither set being permissioned

Order Book

An Early Approach



Decentralized Lending

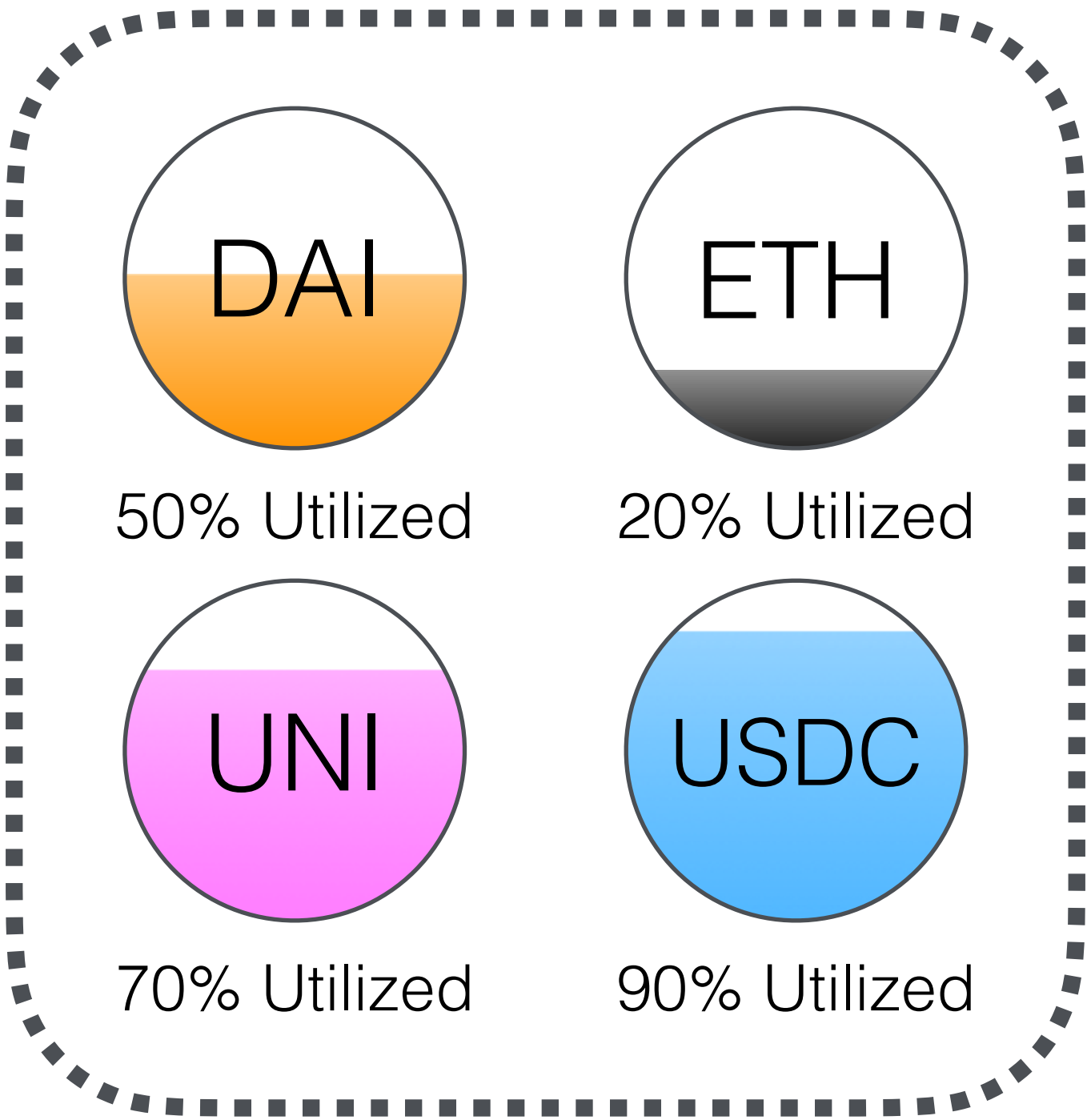
Order Book Defects

- Fractured liquidity
 - More asset pairs thins the supply across those pairs
- Computationally expensive
 - Matching many borrowers or many lenders requires many transactions per person
- Concentrated risk
 - Lenders are exposed strictly to the risk that their matched counter-parties will default, increasing the variance of interest returns
- Fixed rates only
 - As the supply and demand to borrow a given asset changes, matched interest rates don't change, adding complexity
- Difficult withdrawal
 - A supplier must wait for their counter-parties to repay their debts (or force liquidation) to withdraw their share

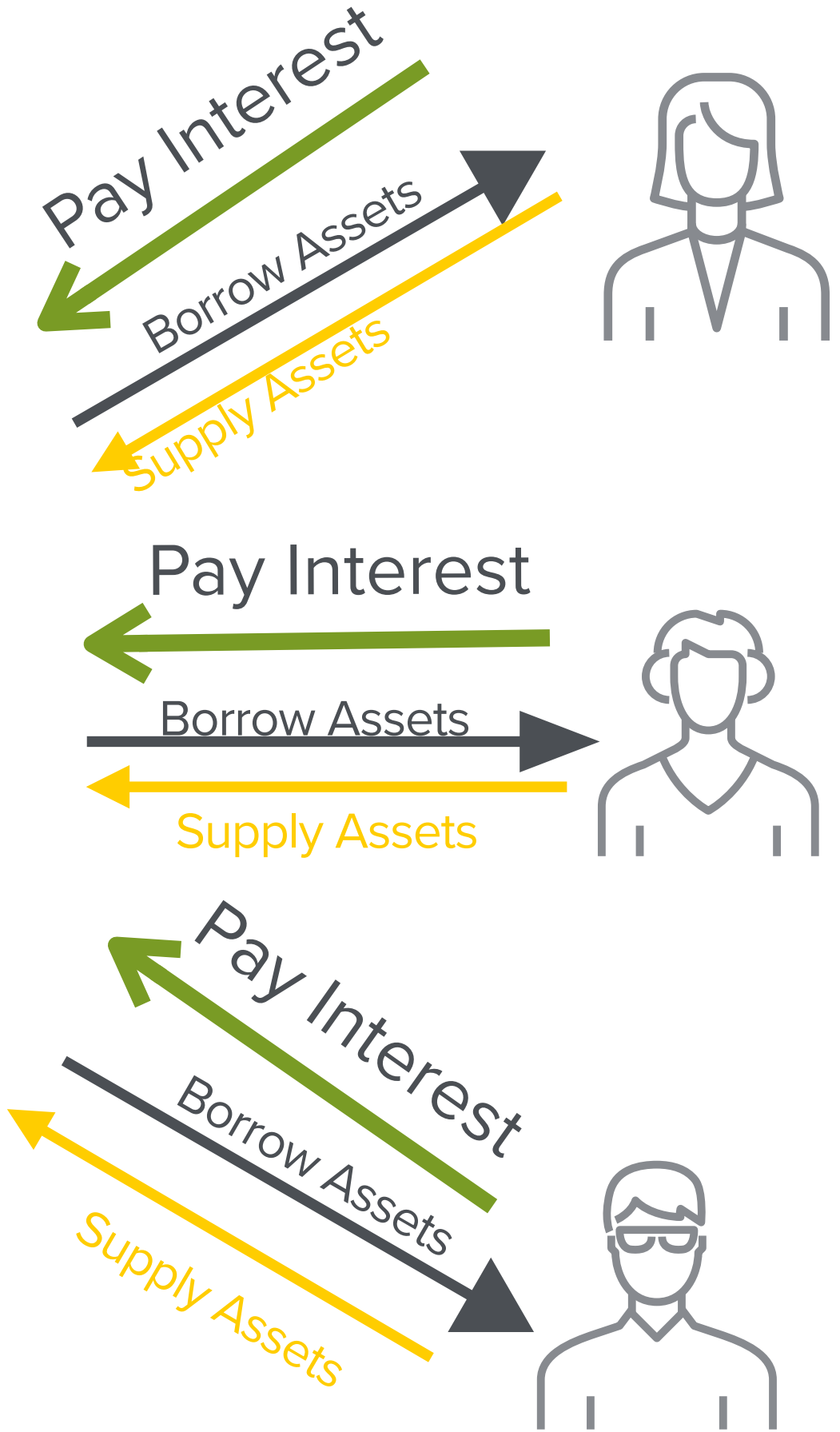
Case Study: Compound

Liquidity Pool Approach

LENDERS



BORROWERS



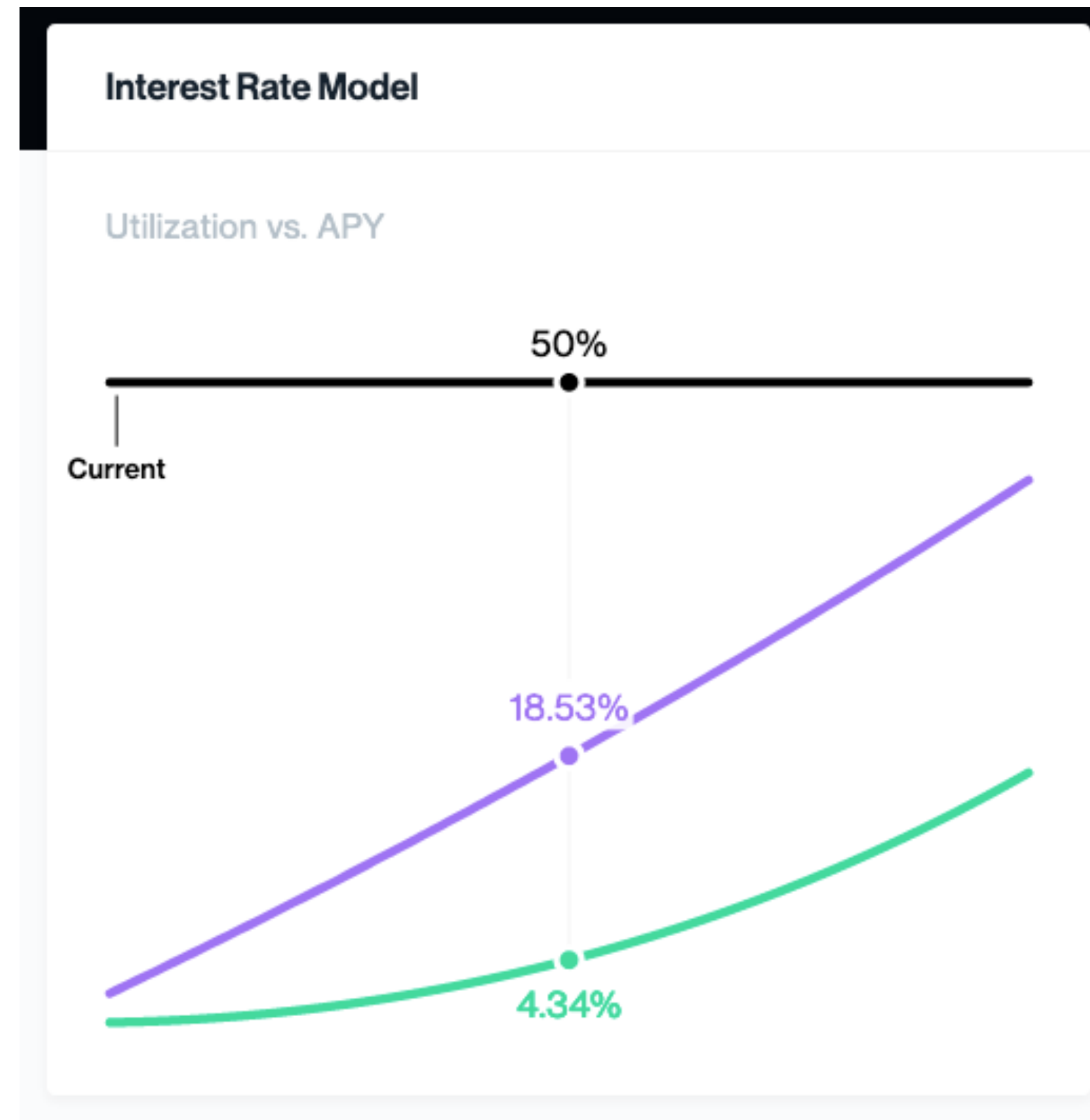
Decentralized Lending

Liquidity Pool Advantages

- Shared liquidity
 - Adding another asset no longer fractures liquidity
- Computationally simpler
 - Suppliers and borrowers can add or remove large volumes with single transactions, independent of the distribution of counter-parties
- Distributed risk
 - Risk is shared by the entire pool*
- Variable rate**
 - An order book matches supply and demand implicitly as borrowers and lenders make adjustments; the shared pool adjusts rates automatically based on existing supply and utilization
- Graceful withdrawal
 - As long as extra assets remain in the pool, a supplier can withdraw their share

Case Study: Compound

Interest Rate Curve for BAT



Utilization Rate
Borrow Interest Rate

Supply Interest Rate

Source: <https://compound.finance/markets/BAT>

Case Study: Compound

Step-by-step Procedure for Borrowing

- Alice supplies 2 ETH to ETH pool
 - Her total ETH-equivalent balance times the **collateralFactor** represents her total capacity to borrow: **sumCollateral**
- Alice requests to borrow 1 ETH worth of BAT
 - Since this is less than her **sumCollateral**, the borrow is valid
- Now, every block, Alice accumulates interest on what she's borrowed until it is repaid

Calculations

- supplied asset
 - 2 ETH
- collateralFactor
 - 0.6
- sumCollateral
 - 1.2
- borrowCurrent
 - 1.0

Case Study: Compound

Utilization Ratio

$$U_a = \textit{Borrows}_a / (\textit{Cash}_a + \textit{Borrows}_a)$$

Utilization Ratio

Case Study: Compound

Interest Rate Curve

$$\text{Borrowing Interest Rate}_a = \text{Base Rate} + U_a * \text{Slope Multiplier}$$



```
function getUtilizationRate(uint cash, uint borrows) pure internal returns (IError, Exp memory) {  
    if (borrows == 0) {  
        // Utilization rate is zero when there's no borrows  
        return (IError.NO_ERROR, Exp({mantissa: 0}));  
    }  
  
    (MathError err0, uint cashPlusBorrows) = addUInt(cash, borrows);  
    if (err0 != MathError.NO_ERROR) {  
        return (IError.FAILED_TO_ADD_CASH_PLUS_BORROWS, Exp({mantissa: 0}));  
    }  
  
    (MathError err1, Exp memory utilizationRate) = getExp(borrows, cashPlusBorrows);  
    if (err1 != MathError.NO_ERROR) {  
        return (IError.FAILED_TO_GET_EXP, Exp({mantissa: 0}));  
    }  
  
    return (IError.NO_ERROR, utilizationRate);  
}
```



```
/*
 * @dev Calculates the utilization and borrow rates for use by getBorrowRate function
 */
function getUtilizationAndAnnualBorrowRate(uint cash, uint borrows) view internal returns (IERError, Exp memory, Exp memory) {
    (IERError err0, Exp memory utilizationRate) = getUtilizationRate(cash, borrows);
    if (err0 != IERError.NO_ERROR) {
        return (err0, Exp({mantissa: 0}), Exp({mantissa: 0}));
    }

    // Borrow Rate is 5% + UtilizationRate * 45% (baseRate + UtilizationRate * multiplier);
    // 45% of utilizationRate, is `rate * 45 / 100`
    (MathError err1, Exp memory utilizationRateMuled) = mulScalar(utilizationRate, multiplier);
    // `mulScalar` only overflows when the product is  $\geq 2^{256}$ .
    // utilizationRate is a real number on the interval [0,1], which means that
    // utilizationRate.mantissa is in the interval [0e18,1e18], which means that 45 times
    // that is in the interval [0e18,45e18]. That interval has no intersection with  $2^{256}$ , and therefore
    // this can never overflow for the standard rates.
    if (err1 != MathError.NO_ERROR) {
        return (IERError.FAILED_TO_MUL_UTILIZATION_RATE, Exp({mantissa: 0}), Exp({mantissa: 0}));
    }

    (MathError err2, Exp memory utilizationRateScaled) = divScalar(utilizationRateMuled, mantissaOne);
    // 100 is a constant, and therefore cannot be zero, which is the only error case of divScalar.
    assert(err2 == MathError.NO_ERROR);

    // Add the 5% for (5% + 45% * Ua)
    (MathError err3, Exp memory annualBorrowRate) = addExp(utilizationRateScaled, Exp({mantissa: baseRate}));
    // `addExp` only fails when the addition of mantissas overflow.
    // As per above, utilizationRateMuled is capped at 45e18,
    // and utilizationRateScaled is capped at 4.5e17. mantissaFivePercent = 0.5e17, and thus the addition
    // is capped at 5e17, which is less than  $2^{256}$ . This only applies to the standard rates
    if (err3 != MathError.NO_ERROR) {
        return (IERError.FAILED_TO_ADD_BASE_RATE, Exp({mantissa: 0}), Exp({mantissa: 0}));
    }

    return (IERError.NO_ERROR, utilizationRate, annualBorrowRate);
}
```



```
/*
 * @dev Calculates the utilization and borrow rates for use by getBorrowRate function
 */
function getUtilizationAndAnnualBorrowRate(uint cash, uint borrows) view internal returns (IError, Exp memory, Exp memory) {
    (IError err0, Exp memory utilizationRate) = getUtilizationRate(cash, borrows);

    // Borrow Rate is 5% + UtilizationRate * 45% (baseRate + UtilizationRate * multiplier);
    // 45% of utilizationRate, is `rate * 45 / 100`
    (MathError err1, Exp memory utilizationRateMuled) = mulScalar(utilizationRate, multiplier);

    (MathError err2, Exp memory utilizationRateScaled) = divScalar(utilizationRateMuled, mantissaOne);

    // Add the 5% for (5% + 45% * Ua)
    (MathError err3, Exp memory annualBorrowRate) = addExp(utilizationRateScaled, Exp({mantissa: baseRate}));

    return (IError.NO_ERROR, utilizationRate, annualBorrowRate);
}
```



```
/*
 * @dev Calculates the utilization and borrow rates for use by getBorrowRate function
 */
function getUtilizationAndAnnualBorrowRate(uint cash, uint borrows) view internal returns (IError, Exp memory, Exp memory) {
    (IError err0, Exp memory utilizationRate) = getUtilizationRate(cash, borrows);

    // Borrow Rate is 5% + UtilizationRate * 45% (baseRate + UtilizationRate * multiplier);
    // 45% of utilizationRate, is `rate * 45 / 100`
    (MathError err1, Exp memory utilizationRateMuled) = mulScalar(utilizationRate, multiplier);

    (MathError err2, Exp memory utilizationRateScaled) = divScalar(utilizationRateMuled, mantissaOne);

    // Add the 5% for (5% + 45% * Ua)
    (MathError err3, Exp memory annualBorrowRate) = addExp(utilizationRateScaled, Exp({mantissa: baseRate}));

    return (IError.NO_ERROR, utilizationRate, annualBorrowRate);
}
```



```
/**
 * @notice Gets the current borrow interest rate based on the given asset, total cash, total borrows
 *         and total reserves.
 * @dev The return value should be scaled by 1e18, thus a return value of
 *      `(true, 1000000000000)` implies an interest rate of 0.000001 or 0.0001% *per block*.
 * @param cash The total cash of the underlying asset in the CToken
 * @param borrows The total borrows of the underlying asset in the CToken
 * @param _reserves The total reserves of the underlying asset in the CToken
 * @return Success or failure and the borrow interest rate per block scaled by 10e18
 */
function getBorrowRate(uint cash, uint borrows, uint _reserves) public view returns (uint, uint) {
    _reserves; // pragma ignore unused argument

    (IError err0, Exp memory _utilizationRate, Exp memory annualBorrowRate) = getUtilizationAndAnnualBorrowRate(cash, borrows);
    if (err0 != IError.NO_ERROR) {
        return (uint(err0), 0);
    }

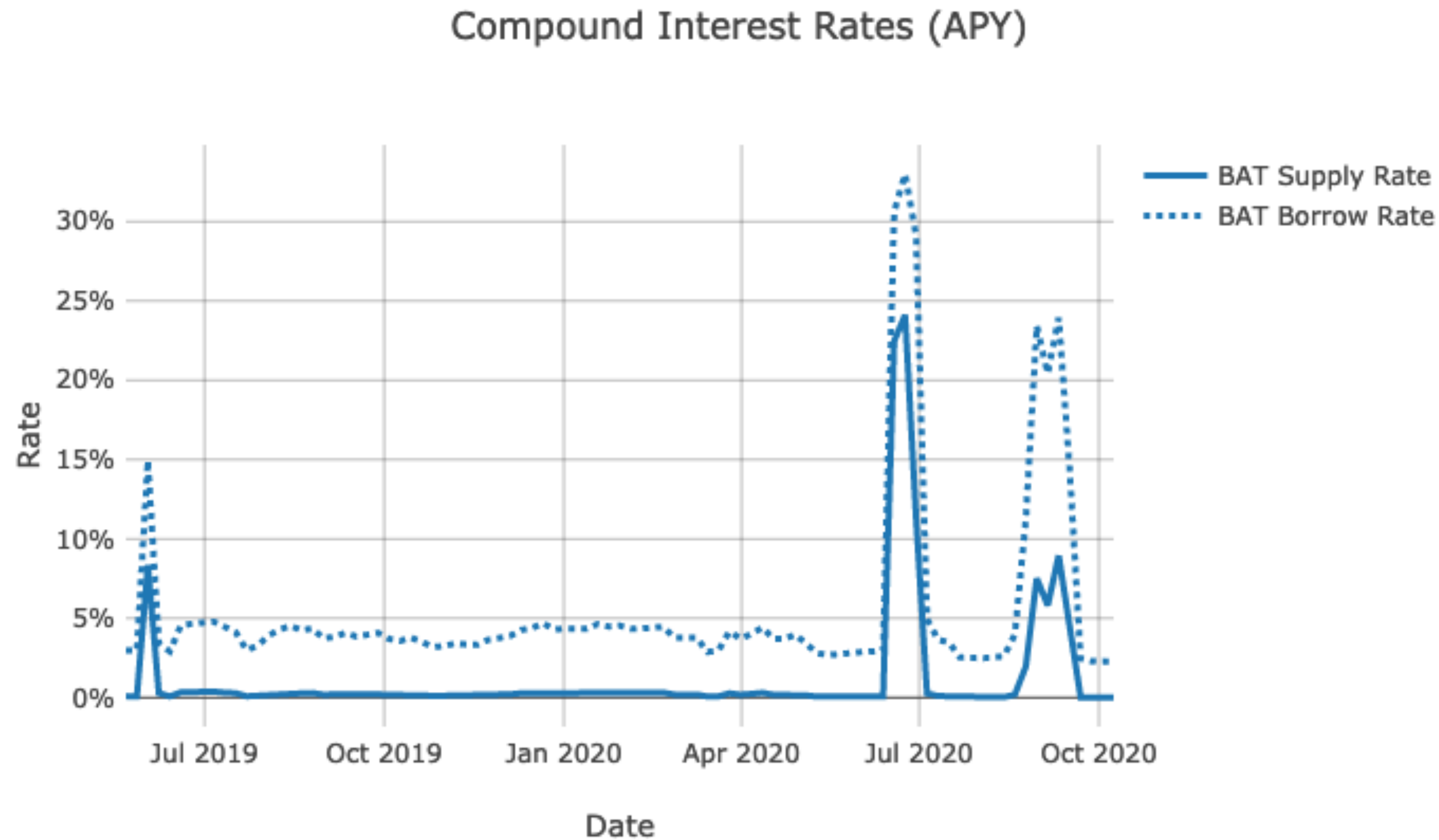
    // And then divide down by blocks per year
    (MathError err1, Exp memory borrowRate) = divScalar(annualBorrowRate, blocksPerYear); // basis points * blocks per year
    // divScalar only fails when divisor is zero. This is clearly not the case.
    assert(err1 == MathError.NO_ERROR);

    _utilizationRate; // pragma ignore unused variable

    // Note: mantissa is the rate scaled 1e18, which matches the expected result
    return (uint(IError.NO_ERROR), borrowRate.mantissa);
}
}
```

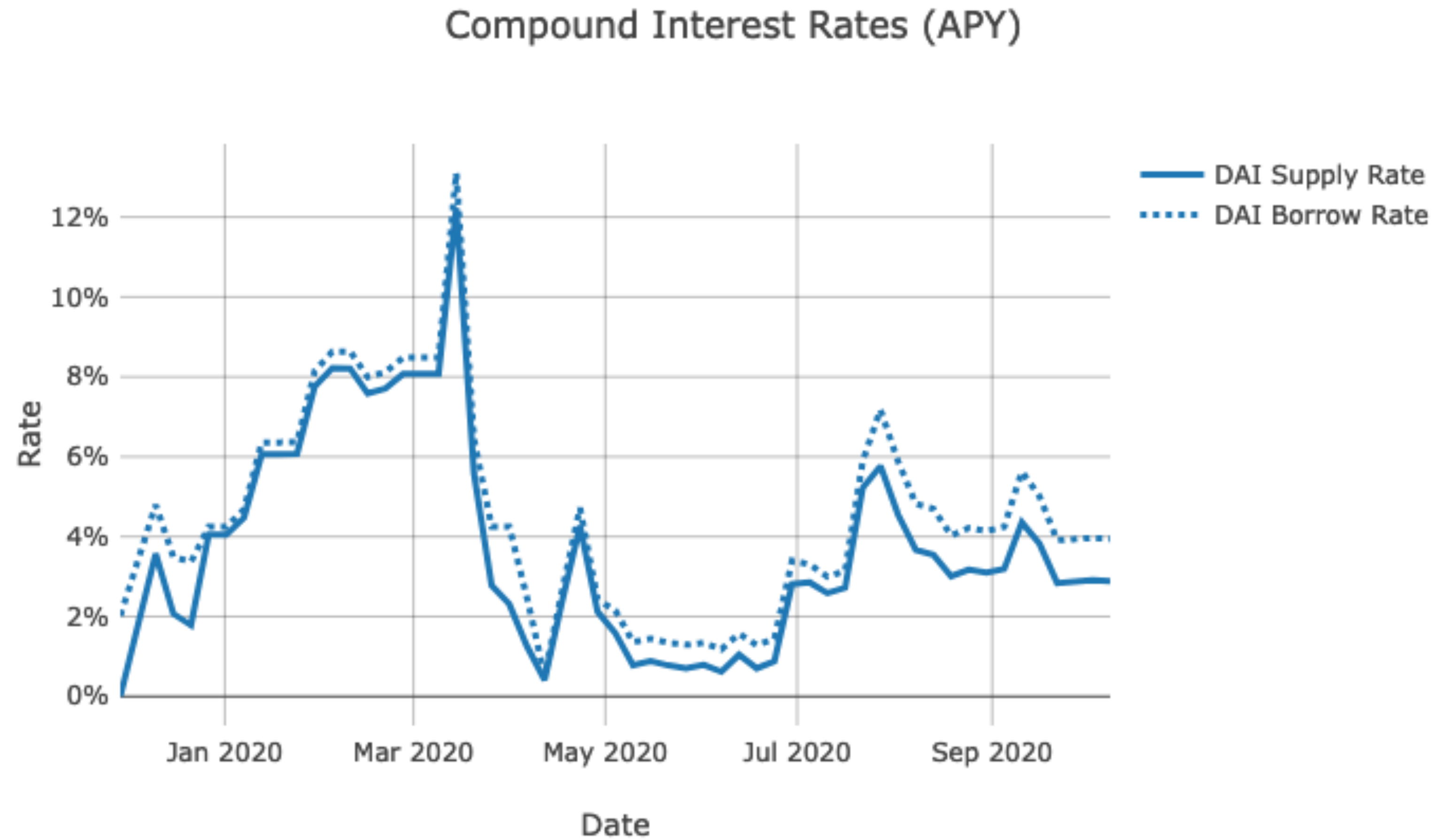
Case Study: Compound

Historical BAT Interest Rate



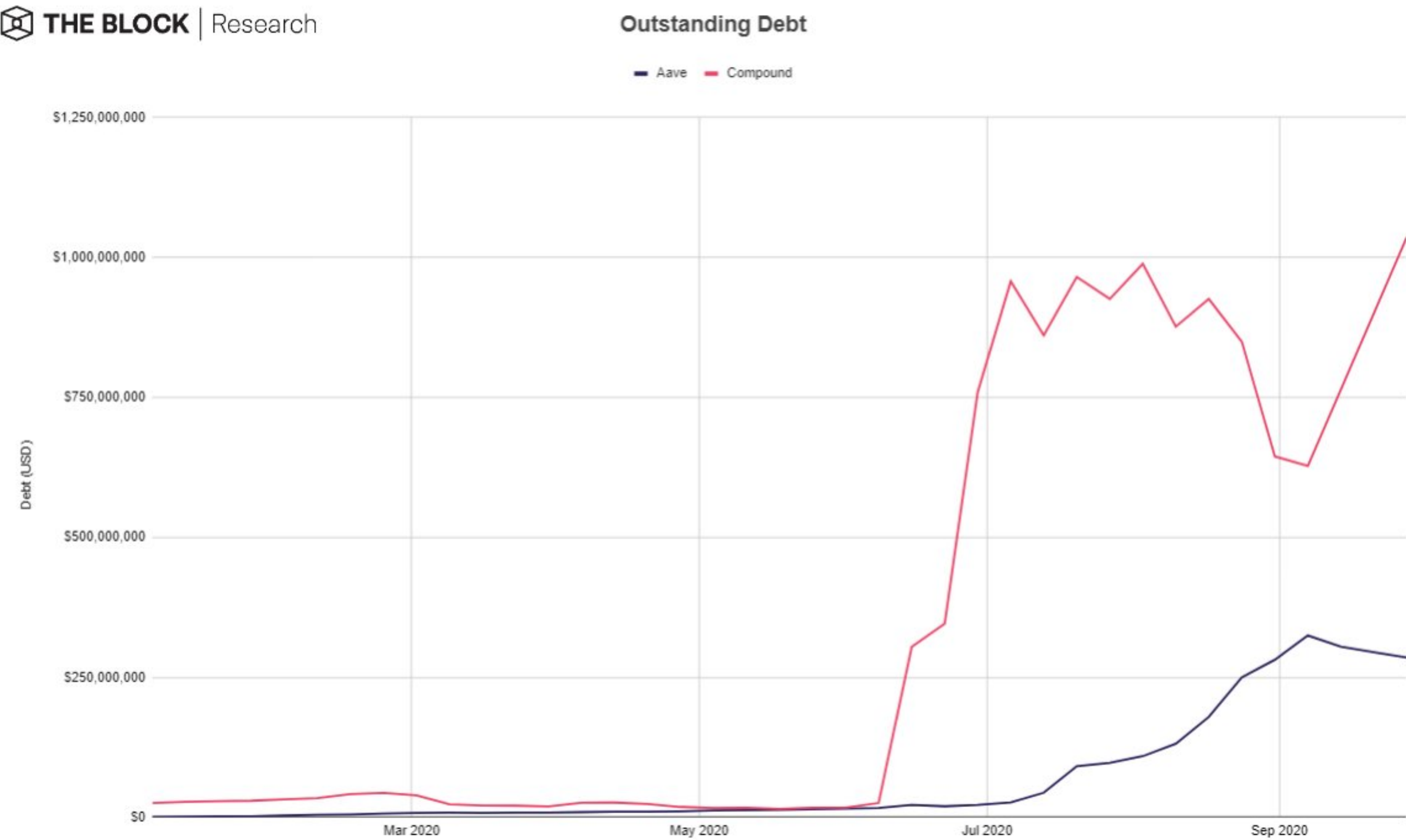
Case Study: Compound

Historical DAI Interest Rate



Case Study: Compound

Historical Borrow



Case Study: Compound

Mechanisms Not Discussed

- cTokens
- The reserve
- Governance
- Incentivized liquidity ("yield farming")
- Liquidation process
- Efforts to support undercollateralized lending

Q & A

Appendix

Links

- Uniswap Whitepaper
 - <https://hackmd.io/@HaydenAdams/HJ9jLsfTz>
- An Analysis of Uniswap Markets
 - <https://arxiv.org/pdf/1911.03380.pdf>
- Understanding Uniswap Returns
 - <https://medium.com/@pintail/understanding-uniswap-returns-cc593f3499e>

Appendix

Links

- Compound Whitepaper
 - <https://compound.finance/documents/Compound.Whitepaper.pdf>
- Compound Docs (can be used to lead you to Etherscan)
 - <https://compound.finance/docs>
- Compound Protocol Github
 - <https://github.com/compound-finance/compound-protocol>
- Compound Protocol Whitepaper Technicals
 - <https://github.com/compound-finance/compound-protocol/blob/master/docs/CompoundProtocol.pdf>